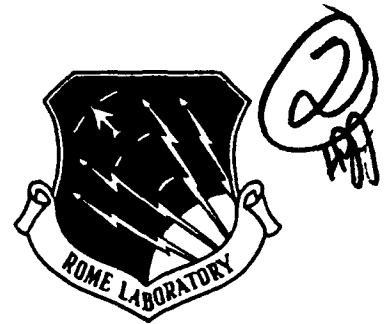


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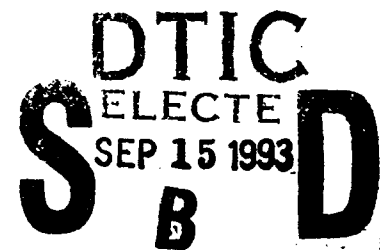


RL-TR-93-115
Final Technical Report
June 1993



PHOTOREFRACTIVE RECEIVER STUDY

Harris Corporation



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Strategic Defense Initiative Office

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APPROVED:



WALTER J. BUSHUNOW
Project Engineer

FOR THE COMMANDER



JOHN A. GRANIERO
Chief Scientist for C3

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PHOTOREFRACTIVE RECEIVER STUDY

M. R. Lange

D. W. Graves

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Principal Investigator: Dr. M. R. Lange
Phone: (407) 727-5119

Project Engineer: Walter J. Bushunow
Phone: (315) 330-3091

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13. ABSTRACT (Maximum 200 words) The Photorefractive Receiver Study was a 12 month study into concepts related to the application of photorefractive materials as adaptive beam combining elements for an optical heterodyne receiver. This study concentrates on the behavior of and requirements for the photorefractive element. A set of parameters and approaches for the photorefractive element was selected and a theoretical model constructed to predict performance. An experiment was designed and fabricated to illustrate the dependencies predicted by the theoretical model. All model and experimental results are described and summarized.					
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Photorefractive Heterodyne Receiver Final Report

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I. Introduction

The following report is the final report on a 12 month study into concepts related to the application of photorefractive materials as adaptive beam combining elements for an optical heterodyne receiver. This study concentrates on the behavior of and requirements for the photorefractive element. As such the models developed and the experiments performed are aimed at quantifying the material requirements.

The experimental parameters chosen for the study are based partly on experience, a literature search, and material and equipment availability. This study was not scoped to investigate multiple approaches. The approach chosen was determined to offer the greatest amount of insight, though not necessarily the best performance. Section II provides insight into available parameters and approaches.

The experiments performed on the study are presented in Section III. They were aimed at illustrating the parameter dependence predicted by the theoretical results presented in Section IV. They also illustrate some of the well known photorefractive parameters dependencies to establish a baseline and demonstrate the performance enhancements by optimizing these parameters. A video tape has been produced on this program illustrating one of the key advantages of the photorefractive beam combiner, platform jitter compensation. This is discussed in Section III.

Heterodyne gain is the topic of Section IV. The modeling performed on this study is outlined in Section IV and the most significant results presented. The purpose of this section is to illustrate the requirements of the photorefractive beam combiner for receiver applications. The analysis is primarily oriented towards illustrating the advantages, disadvantages, and limitations of a photorefractive beam combiner from a systems point of view. A discussion of heterodyne reception begins below in the current section in order to lay the groundwork for the following sections.

Conclusions and recommendations are presented in the final section. There are several new developments in materials technology which open new possibilities for photorefractive elements. These are discussed and conclusions are drawn as to their potential for application to heterodyne reception.

Heterodyne techniques

Heterodyne signal reception has been a widely used concept since the early days of radio. A heterodyne receiver utilizes a local oscillator to mix with the received signal to enhance the signal reception. Optical heterodyne receivers work in a similar manner for similar reasons. At the radio carrier frequencies heterodyne reception is a common practice.

An optical implementation of this is not common in operational systems.

There are several difficulties in implementing heterodyne techniques at optical carrier frequencies due to the high optical frequencies (short wavelengths). The first obvious difficulty is that optical sources are not typically stable down to frequencies usable for signal transmission and reception. This is quickly changing, though. New solid state diode pumped lasers are commercially available with linewidths in the kiloHertz.

Given narrow line laser technology, the frequency of the transmitter must still be tracked by the receiver. This can be done by getting the signals close enough for the receiver to acquire the transmitter frequency and then track it. It may be possible to lock the transmitter and receiver to some known absolute frequency source (atomic lines under controlled conditions) and electronically track out residual errors that may exist.

The next difficulty encountered is in collecting the signal and combining it coherently with the oscillator. It can be difficult to collect the transmitted light and combine it coherently with a local source if it has suffered any significant phase front degradation. One can sample smaller and smaller cross sections of light until sufficient phase front integrity is obtained at the cost of collecting less light. Or one can try to compensate for the phase front errors. Another difficulty related to the short wavelength is that small motion or vibration cause many wavelength shifts in position, and thus can cause noise or further demands on the frequency tracking.

A significant increase in complexity of a system results from the requirements of an optical heterodyne technique, over a system that utilizes direct detect techniques. One must, therefore, ask for a clear quantification of the benefits of this increased complexity.

The performance of a receiver is limited by the signal-to-noise-ratio out of the receiver. The ultimate performance of an optical receiver is realized in the signal to shot noise received (a photon noise limited system). If the shot noise is the dominant noise term then that is the best performance that particular receiver can have for a given signal level. A large local oscillator used for heterodyne detection of a small received signal will necessarily degrade the shot noise limited signal-to-noise-ratio of the receiver output compared to a direct detect system. The primary advantage offered by an optical heterodyne technique is in bringing a weak signal up to the shot noise limited region of the detector. That is, if the detector is, for example, thermal noise limited with the incident signal level, a sufficiently large local oscillator mixed with this signal will produce a large cross product term on the detector and bring the signal up to shot noise limited performance.

The key issues that evolved in this study relevant to the performance limitations of the photorefractive beam combiner for heterodyne reception are discussed in Section IV below. Several of the significant issues discussed are; arbitrarily large pump sources cannot be used in a photorefractive beam combiner to increase signal gain, optical attenuation in the photorefractive material can be a severe limitation, and photorefractive gain-bandwidth is a

critical figure of merit for a heterodyne beam combiner application.

II. Parameter Study

A literature survey of experiments conducted for photorefractive gain measurements was performed on this study. The results are presented below in tabular form. There is a large array of experimental approaches to achieving photorefractive gain in several different materials. The materials emphasized in this study are the fast response time materials, comprised mostly of semiconductors.

A detailed theory of these materials can be found in the references and will not be presented here. The goal here is to illustrate the range of parameters achievable as determined by leading experimenters in the field. These parameters will then be used for comparison of the various approaches with respect to an optical heterodyne receiver applications.

Note in the first column of the table is a reference to the technique used to achieve photorefractive gain. These various techniques are explained in great detail in the references, so that level of explanation is not offered here. The general idea involved is that when the incident optical intensity pattern has a certain phase with respect to the forming refractive index grating the light will be preferentially diffracted along one path and the reinforcement of light intensity will cause the grating to exponentially grow along the path of light diffraction until the light in the other path that helped form the initial grating becomes depleted. Thus, the smaller the initial light component is in the preferential path, the larger the gain potential. Here gain is defined as the ratio of light level, after passing through the crystal, with and without the interferer present.

The second column lists the material band-gap for comparison with the wavelength utilized. The third column shows the time response of the interaction. Most of these are estimates based on scaling relationships and are here for reference only. Gain coefficient, gain, and loss (optical attenuation) are shown in the fourth column of the table, in addition to spatial modulation wavelength and bias voltage. The wavelength of the interaction is shown in the last column along with the beam ratio, with reference to the first author on the work.

This table is not all inclusive, but a sampling of some of the better experimental measurements of gain. All of these parameters were used in the models developed below to estimate their performance as a beam combining element for a receiver application. This provides a range of potential beam combiner parameters in order to develop an understanding of potential performance that might be obtained with materials currently available.

TABLE II-1 Gain measurements

Material	Bandgap	Time response	Gain Coeff. loss (gain)	Wavelength Beam Ratio
CdTe:V (AC bias) 200 kHz	1.56 eV (0.8 μ M)	4. ms @ 1 W/cm ² est	3.3 cm ⁻¹ , 4.mm 0.8 cm ⁻¹ (3.7) @ 5.5 μ M, 10kV/cm	1.32 μ M Ziari
GaAs:Cr (moving fringes) 50 Hz	1.42 eV (0.87 μ M)	40. ms @ 0.05 W/cm ² meas	6.5 cm ⁻¹ , 3.6mm 1.65 cm ⁻¹ (10) @ 18 μ M, 8.6kV/cm	1.064 μ M 1000/1 Imbert
InGaAs:EI2 (Franz-Keldysh moving fringe) 4 Hz	1.42 eV (0.87 μ M)	340. ms @ 0.140W/cm ² est	16.3 cm ⁻¹ , 4.mm 3 cm ⁻¹ (600) @ 7 μ M, 10kV/cm	0.94 μ M 4800/1 Partovi
GaAs:EI2 (trap saturation)	1.42 eV (0.87 μ M)	30. ms @ 0.013W/cm ² est	2.6 cm ⁻¹ , 6.mm 1.3 cm ⁻¹ (4.7) @ 9 μ M, 13kV/cm	1.064 μ M 60/1 Duncan
GaAs:EI2 (AC bias) 20 kHz	1.42 eV (0.87 μ M)	10. ms @ 0.02 W/cm ² calc	2.4 cm ⁻¹ , 10.mm 0.87 cm ⁻¹ (11) @ 15 μ M, 3.2kV/cm	1.064 μ M 10 to 1000/1 Klein
InP:Fe (trap saturation)	1.35 eV (0.92 μ M)	30 ms @ 0.03 W/cm ² meas	4. cm ⁻¹ , 4mm 2. cm ⁻¹ (5) @ 5 μ M, 8kV/cm	1.064 μ M 80/1 Mainguet
InP:Fe (thermal balance) (grad)	1.35 eV (0.92 μ M)	150. ms @ 0.009 W/cm ² est	6.5 cm ⁻¹ , 7.2mm 2.6 cm ⁻¹ (100) @ 5 μ M, 10kV/cm	1.064 μ M 8000/1 Ozkul
InP:Fe (incoherent backlight)	1.35 eV (0.92 μ M)	60. ms @ 0.015 W/cm ² est	4.7 cm ⁻¹ , 7.2mm 2.6 cm ⁻¹ (30) @ 5 μ M, 10kV/cm	1.064 μ M 1500/1 Ozkul
InP:Fe (AC bias) 400 Hz	1.35 eV (0.92 μ M)	0.58 ms @ 0.03 W/cm ² meas	2.5 cm ⁻¹ , 9.1mm 0.15cm ⁻¹ (9.7) @ 25 μ M, 10kV/cm	1.32 μ M 80/1 Bylsma

Material	Bandgap	Time response	Gain Coeff. loss (gain)	Wavelength
InP:Fe (Franz-Keldysh thermal balance)	1.35 eV (0.92 μM)	60 ms @ 0.07 W/cm ² est	19 cm ⁻¹ , 2.2 mm; 5 cm ⁻¹ (65) @ 8.5 μM , 10 kV/cm	0.97 μM 1000/1 Millerd
BSO (moving fringes)	3.2 eV (0.4 μM)	100 ms @ .01 W/cm ² meas	3.6 cm ⁻¹ , 10 mm @ (6) 23 μM , 10 kV/cm	0.568 μM 2000/1 Hamel de Monc.
InP:Fe (thermal stabilized)	1.35 eV (0.92 μM)	10 ms @ 0.09 W/cm ² est	5.3 cm ⁻¹ , 7.2 mm; 0.5 cm ⁻¹ (45) @ 5 μM , 10 kV/cm	1.32 μM 700/1 Ozkul 2
InP:Fe (thermal stabilized)	1.35 eV (0.92 μM)	10 ms @ 0.09 W/cm ² est	8. cm ⁻¹ , 4. mm 2.3 cm ⁻¹ (25) @ 6 μM , 10 kV/cm	1.06 μM 570/1 Ozkul 2

III. Experimental Results

Experimental Background

The literature search mentioned above revealed several ways of enhancing the photorefractive gain in semiconductor materials used by other researchers. Because of the small electro-optic coefficient in the faster response time materials application of an external electric field across the photorefractive crystal is a common practice to enhance photorefractive effects. When the external electric field remains constant the photorefractive grating within the crystal drifts, due to dynamic charge migration, along the direction of the electric field. This drift can be adjusted to coincide with the drift of the optical fringes produced from two optical beams offset from each other by a small frequency difference. When these coincide, a 90 shift occurs between the optical fringe pattern and the photorefractive grating. The light interference then reinforces the charge grating in a positive feedback mode and exponential growth of the grating intensity results. The photorefractive effect is maximized and one of the light paths will experience gain.

Two coherent beams offset by a small frequency shift can be easily created with a single laser and several acousto-optic Bragg cells. The first Bragg cell, driven by a frequency w_1 , separates the laser beam into two beams. The undiffracted light serves as the pump beam, while the diffracted light will be further diffracted by the second Bragg cell to contain a modulated signal for detection. The undiffracted beam can be set several orders of magnitude stronger than the diffracted beam. The frequency of the diffracted beam has been Doppler shifted by the Bragg cell drive frequency, and is represented by $W + w_1$. The second Bragg cell adds a modulated signal to the beam. The Bragg cell Doppler shifts the light by its drive frequency w_2 , resulting in a frequency of the beam of $W + w_1 - w_2$. The negative of the second Doppler shift term comes from Doppler shifting the optical beam down in frequency by the incidence of light in the direction of the acoustic wave. When the two frequencies w_1 and w_2 are equal then the resulting beam is perfectly phase coherent with the pump beam. A net shift in frequency occurs when the two frequencies are offset by a small amount and the modulated beam is then shifted in frequency relative to the pump beam. If this beam interferes with the pump beam the resulting light fringe will move spatially at a velocity proportional to the frequency difference between the two beams.

The modulated signal in the second Bragg cell can be simulated in a number of ways using two frequencies present in the cell simultaneously. Two frequencies summed together produces a single sideband modulated tone. Mixing the two frequencies together generates a double sideband signal with the carrier frequency amplitude determined by the voltage offset of the modulating component. We have chosen to use a single sideband modulation scheme in the experiment for simplicity. One frequency is nearly identical in frequency to the frequency driving the first cell, and the second frequency, offset by about 150 KHz, represents the signal sideband containing the modulation information. These two signals, referred to as the reference and signal beams respectively, interfere at the detector to produce

a 150 KHz tone whose strength is determined by the cross product term of the individual amplitudes. This signal will be detected regardless of any photorefractive processes or lack thereof. The goal of the experiment is to interact the reference beam with the pump beam in the photorefractive crystal, deflecting some of the pump beam into the reference beam. This will increase the amplitude of the reference beam and the cross product term at the detector for a heterodyne detection gain.

Establishing and verifying a number of relationships upon which the photorefractive gain is dependent comprised the bulk of the experimental work. Pump intensity, reference intensity, and signal beam intensity and the relative intensities between the three beams all determine the strength and bandwidth of the photorefractive gain resonance. Additionally the gain is related to the angle of incidence between the reference and pump beams, electric field applied to the crystal and the frequency offset between the reference and pump beams. Other aspects of the photorefractive process such as vibration and aberration correction and resonance bandwidth were investigated.

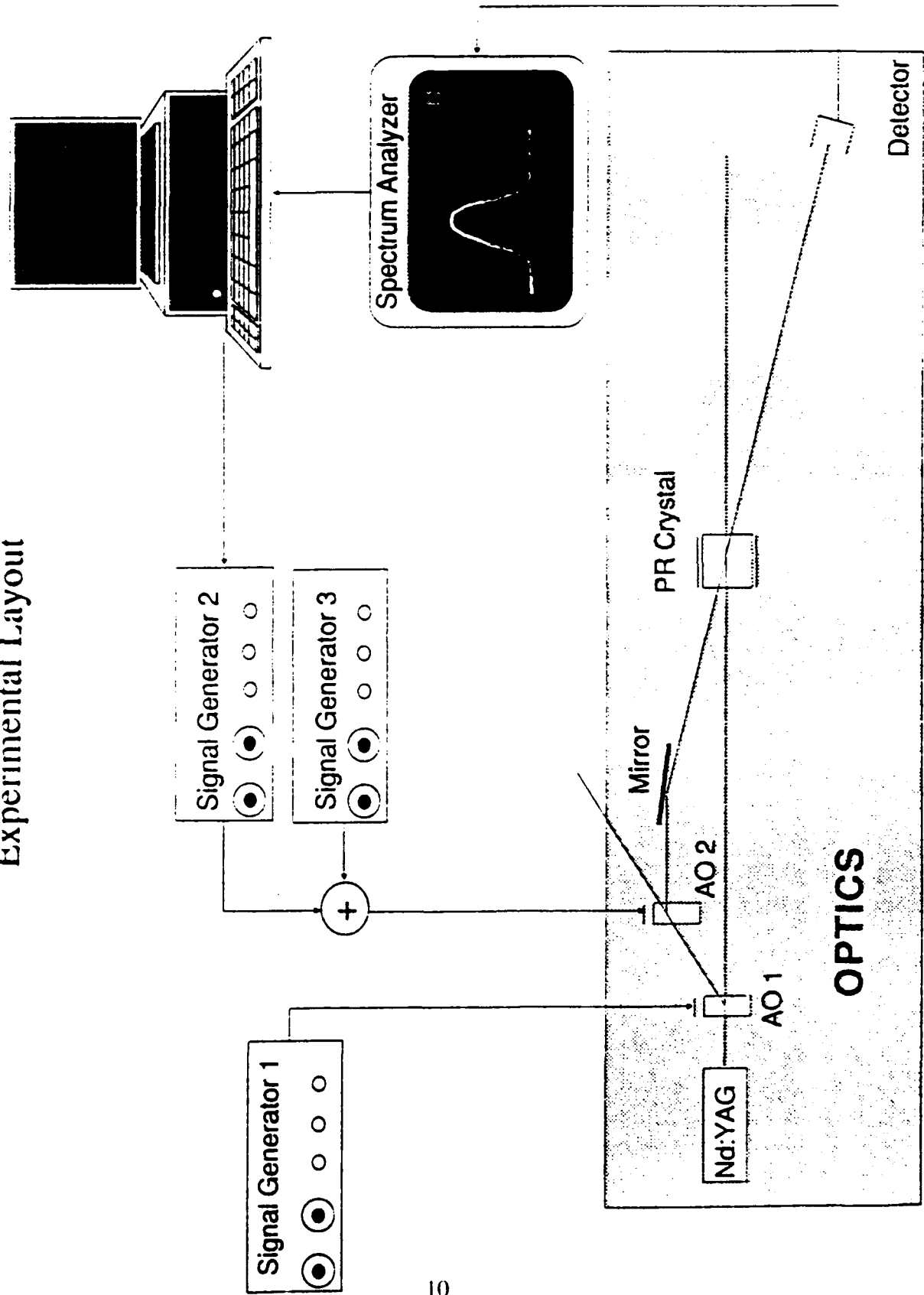
Experimental Test Setup

Figure III-1 shows a block diagram of the experimental setup. Three signal generators, operating off a common clock to ensure relative stability, drive the two Bragg cells. Signal generator 1 drives Bragg cell 1, used to separate the reference and signal beams from the pump beam. Signal generators 2 and 3 drive Bragg cell 2, simulating a single side band modulated optical beam. Generator 2 creates an optical beam we call the reference, and generator 3 creates the signal beam. The output of generators 2 and 3 are summed together before entering the Bragg cell. The optical beams interact in the photorefractive crystal and a In:GaAs detector collects the resulting intensity modulated signal which is fed into a spectrum analyzer. The computer records the peak measured by the spectrum analyzer in a data file.

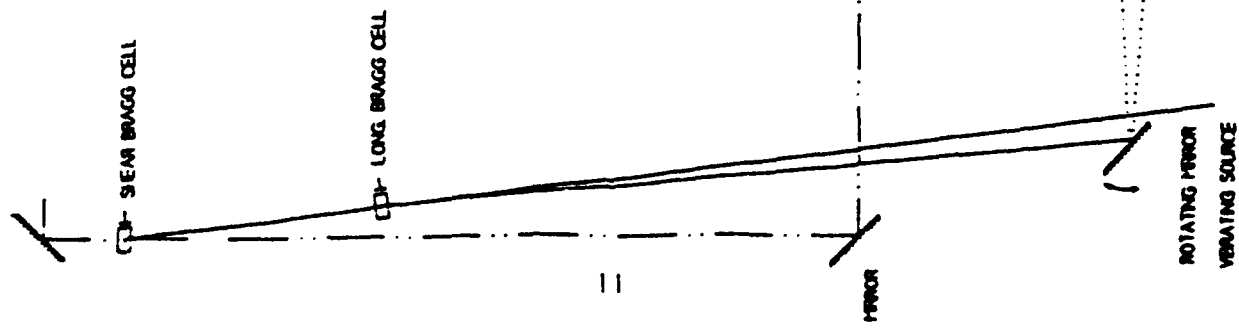
Figure III-2 shows a more detailed layout of the optical system. We used a Nd:YAG (1.06 μm) laser because of its stability and very narrow line width. The only laser available during these experiments at 1.3 microns was a laser diode. This laser would not give a large enough coherence length (approximately 0.3 mm) to operate a dual leg interferometer. All data presented in this report were taken at 1.06 microns.

To obtain a large enough deflection angle at 70 MHz to sufficiently separate the pump beam we used a shear TeO_2 cell for Bragg cell 1. The polarized light of the laser rotates in this cell due to the optical activity of TeO_2 in the optical direction. This angle of rotation is sensitive to temperature and thus to drive power. A linear polarizer placed immediately following the Bragg cell ensures the polarization of all optical beams in the [1 1 0] plane of the photorefractive crystal. Since the polarization of the optical beam is sensitive to Bragg cell temperature, the resulting optical intensities were sensitive as well, and sometimes not repeatable. Standard operating practice was to turn on the Bragg cell well before taking any data and make no adjustments in drive power to the cell thereafter.

Experimental Layout



OPTICAL LAYOUT - PRHR



III-2 Optical layout

The pump beam travels through the system until it reaches a magnifying pair of cylindrical lenses that increased the beam size 10x in the horizontal direction before entering the photorefractive cell allowing the pump beam to completely illuminate the cell from one electrode to the other thus limiting the possibility of shadowing effects. The reference and signal beams are generated with a longitudinal TeO₂ cell (no optical activity). A mirror that can be either rotated to provide variable incidence angles at the photorefractive cell, or vibrated to study the vibration and aberration compensation of the system, folds the optical path to follow the optical table. The reference and signal beams then pass through two cylindrical lenses that provide a 1x magnification in the spot size. The magnifying lenses (1x for the reference and signal and 10 x for the pump) share a common Fourier plane in which a folding mirror is placed in the pump beam. This allows the reference and signal to pass through the photorefractive crystal at small angles relative to pump, about 2 degrees. A detector is placed beyond the photorefractive crystal to detect the intensity modulation produced by the cross product of the reference and signal beams.

Single carrier model

Experiments performed with this setup were designed to measure and verify some of the theoretical receiver calculations described in Section IV of this report. In addition, some of the common measurements made on photorefractive materials were made to verify a baseline of initial assumptions about the material. The basis of the photorefractive calculations comes from several equations governing the behavior of single carrier photorefractive crystals. Although it has been shown that a two carrier model is required to describe the behavior of photorefractive InP, the single carrier model^(Stepanov) is sufficient to explain trends in many limits. These equations are described here with application to the experiments to describe general trends observed, not to quantify the data. Verification of assumptions of the heterodyne receiver model of Section IV were also made.

The magnitude of light diffraction efficiency due to the index grating is

$$\eta \propto \left(\frac{1}{2} n^3 r_{eff} E_{\pi} \right)^2 \quad (1)$$

in the small diffraction limit where n is the applicable refractive index and r_{eff} is the effective electro-optic coefficient. This proportionality is independent of grating phase in the small diffraction limit. The static index grating is generally produced by a space charge electric field developed due to charge separation, and is given by,

$$E_x = - \frac{mE}{1 + K^2 l_s^2 - iK l_g} \quad (2)$$

in the applicable limits where diffusion effects are small compared to charge drift from the bias field. The material response time, ignoring diffusion effects, is given by the equation,

$$\tau_x = \frac{\tau_M (K^2 r_D^2)}{(1 + K^2 r_D^2)(1 + K^2 l_s^2) + K^2 r_D^2 l_s^2} \quad (3)$$

where,

$$\tau_M = \frac{e}{\sigma} \dots \dots \dots \text{Maxwell relaxation time}$$

$$K = \frac{2\pi}{\Lambda} \dots \dots \dots \text{Spatial grating frequency}$$

$$r_E = \mu \tau E \dots \dots \dots \text{carrier drift length}$$

$$l_s = \sqrt{\frac{ek_B T}{e^2 N_A}} \dots \dots \dots \text{Debye screening length}$$

$$l_g = \frac{eE}{eN_A} \dots \dots \dots \text{electron tightening length}$$

and the notation and definitions are from Stepanov et. al. In many cases of interest the Debye screening length l_s can be neglected. Trap saturation in the absence of an applied electric field is uncommon under usual experimental conditions.

By offsetting the reference and pump beam frequencies the grating can be made to

drift along the electric field and the maximum space charge field becomes

$$E_{sc} = \frac{-imEKr_E}{1 + K^2r_D^2 - K^2r_E^2} \quad (9)$$

At resonant frequency

$$v_o = \frac{r_E - l_E(1 + K^2r_D^2)}{\tau_M(K^2r_E^2)} \quad (10)$$

These equations illustrate the response of a single carrier photorefractive crystal for various electric fields, pump intensities, and reference beam - pump beam relative incident angles. The resonant velocity is dependent on electric field, relative angle between beams, and pump beam intensity.

The experimental setup has the capability of independently adjusting the reference beam intensity, signal beam intensity, pump beam intensity, electric field applied to the photorefractive crystal, angle of incidence of the reference and signal beams relative to the pump beam, and the frequency offset between the reference and pump beam. In addition, three different samples of indium phosphide were used to compare various absorption coefficients within the crystals. This section presents our findings on the impact of each individual variable on the operation of the system for the conditions described.

A typical 'dataset' is collected as follows: The signal generator 1 is preset to 70 MHz. Signal generator 2 is set to 70 MHz and signal generator 3 is set to 69.85 MHz. Once the spectrum analyzer has locked on to the 150 KHz beat between the reference and signal beams, the computer changes signal generator 2 to a different frequency several KHz off 70 MHz. Typical offsets are 2 to 6 KHz. The computer then waits for the spectrum analyzer to obtain and measure the shifted signal. Once the spectrum analyzer reports a data point to the computer the signal generator is then stepped in frequency by a small amount and the computer again waits for the spectrum analyzer to complete its measurement. The computer tracks the frequency of signal generator 2 and the peak value of the signal from the spectrum analyzer and stores this information on a file from which we can construct signal versus

frequency offset plots.

After assuring ourselves that the data we were taking were accurate and meaningful we began investigating the many variables built into the system to understand the relationship between the gain of the system and/or the bandwidth, and the heterodyne gain.

Pump beam intensity

The pump beam is typically several orders of magnitude more intense than the other beams, and hence dominates the number of photoelectrons within the crystal. The Maxwell relaxation time is inversely proportional to the photoelectron density, which in turn is proportional to pump intensity and absorption rate. The response time of the grating is directly related to τ_M , and thus we should expect to see a faster response time as the pump intensity increases. The resonant velocity on the other hand is inversely proportional to τ_M , and we would then expect to see the resonant velocity increase with pump power.

Figure III-3 is a composite plot of several data sets taken with different pump intensities. Each curve shows the shape of the resonance produced with the pump intensity adjusted to the amount annotated on the graph. The abscissa is plotted as frequency offset (between reference and pump beams), which is simply Kv_0 , the product of the grating vector and the velocity. The ordinate represents the peak signal intensity detected by the photodetector and measured by the spectrum analyzer. The response time of the grating can be determined from the plots by noting that the response time is the inverse of the bandwidth. The trends apparent in this figure are that the bandwidth decreases with decreasing pump intensity and the resonant velocity decreases with decreasing pump intensity. This is consistent with predictions. Note that the signal output does not scale as the pump intensity. This is as predicted by the model in the following section. This behavior is quite different from an optical heterodyne receiver that utilizes a conventional beam combiner. This is discussed further in Section IV. Figure III-4 shows another plot of the bandwidth dependence. The different curves represent data taken with various grating wavelengths.

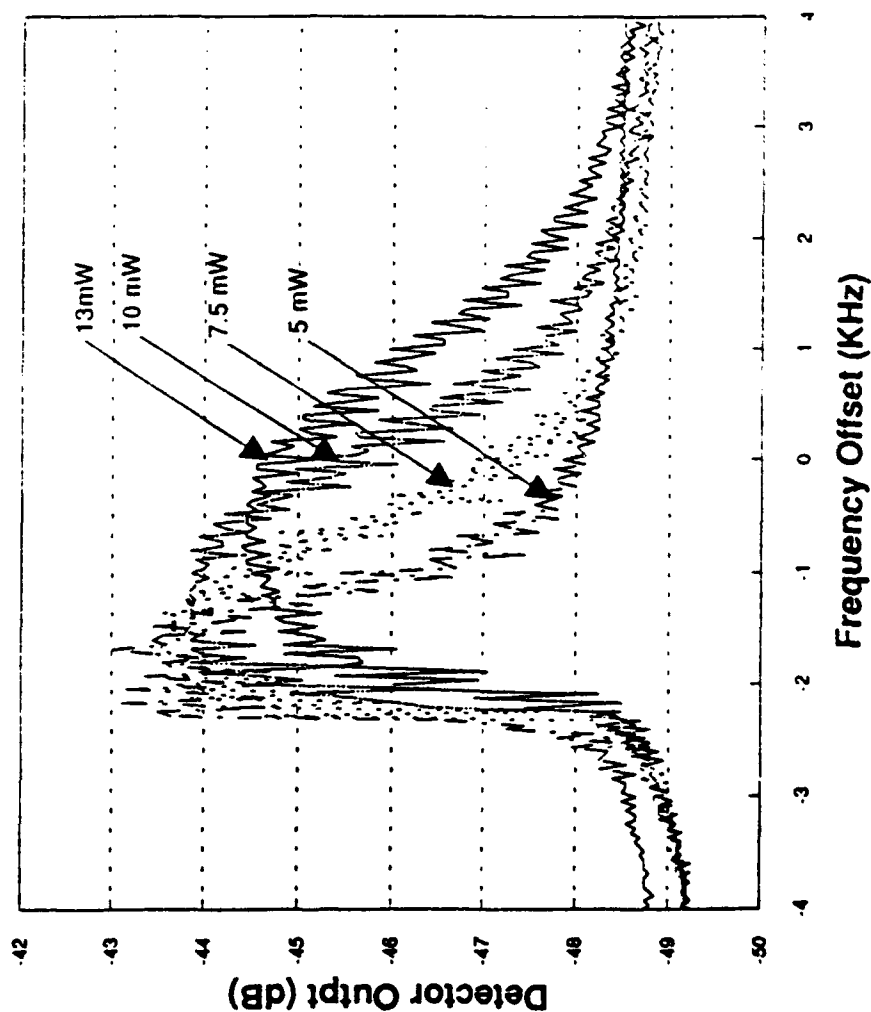
Electric field

The electric field manifests itself in the equations through the drift length r_E , and the electron tightening length l_E , as well as being explicitly found in the amplitude equation. E_{sc} is to first order proportional to the electric field applied. As the saturation point is reached, $K^2 r_E l_E$ dominates the denominator and we find the grating amplitude to be essentially independent of electric field. Figure III-5 shows the peak signal plotted versus electric field strength. An increase in signal strength versus electric field strength is shown up to the maximum voltage of 3200 volts. This demonstrates that the photorefractive devices are operated in the non-saturated mode.

The resonant velocity should decrease with increasing electric field since E is dominant in the denominator. Figure III-6 shows a plot of how the applied electric field

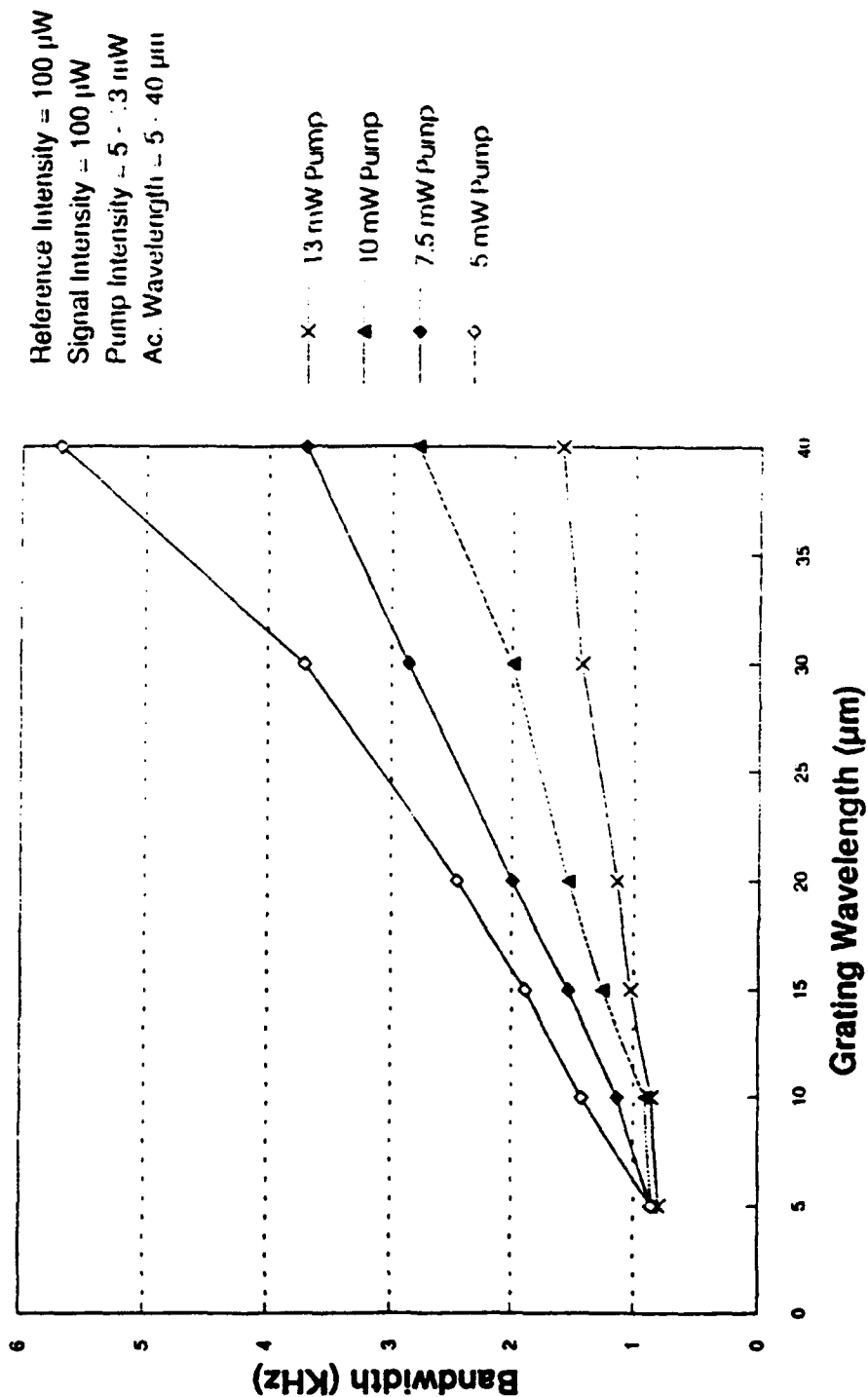
Effect of Pump Intensity on Amplitude and Bandwidth

Reference Intensity = 100 μ W
 Signal Intensity = 100 μ W
 Pump Intensity = 5-13.5 mW
 Ac. Wavelength = 30 μ m



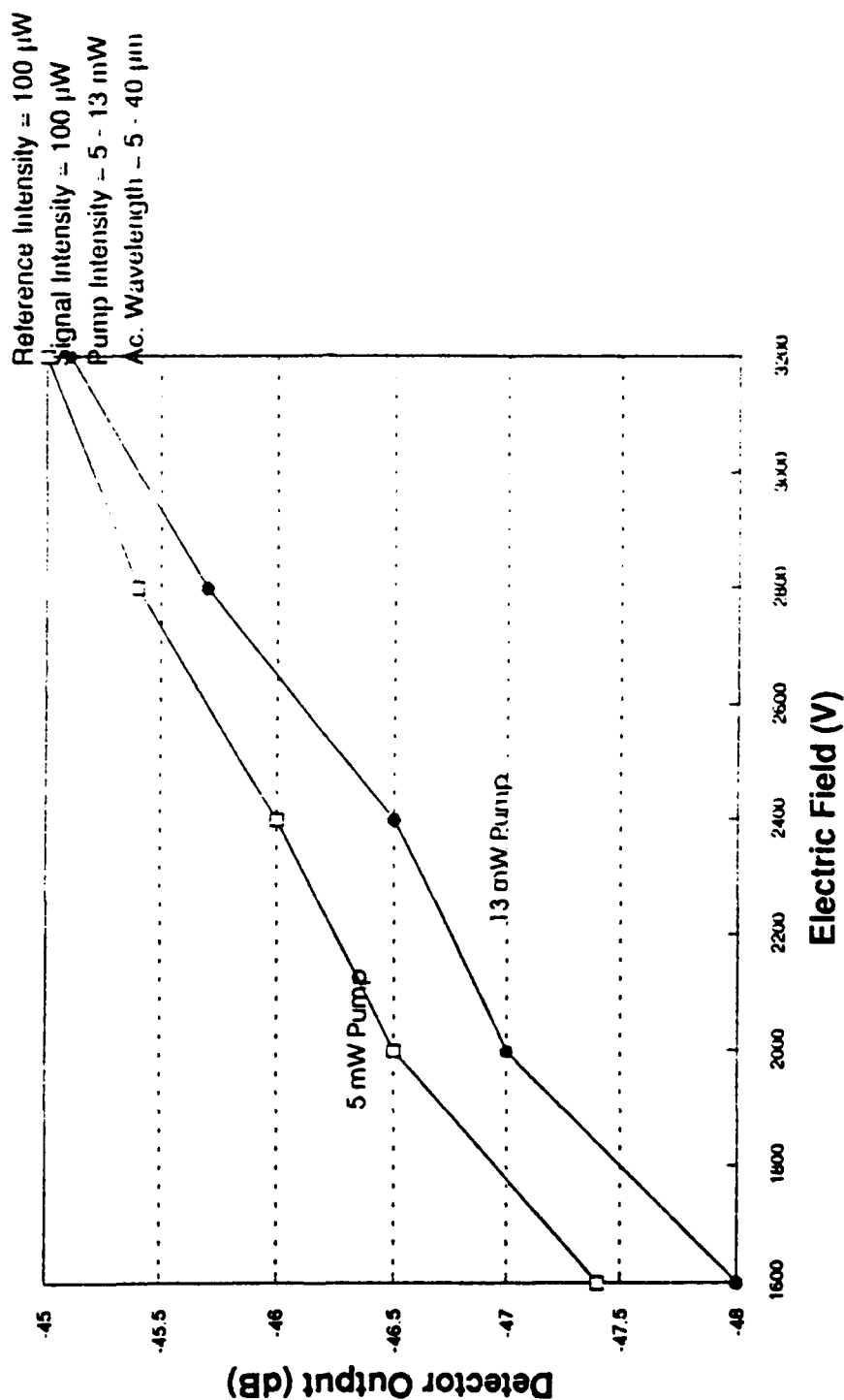
III-3 Effect of pump intensity on amplitude and bandwidth

Effect of Pump Intensity and Grating Wavelength on Bandwidth



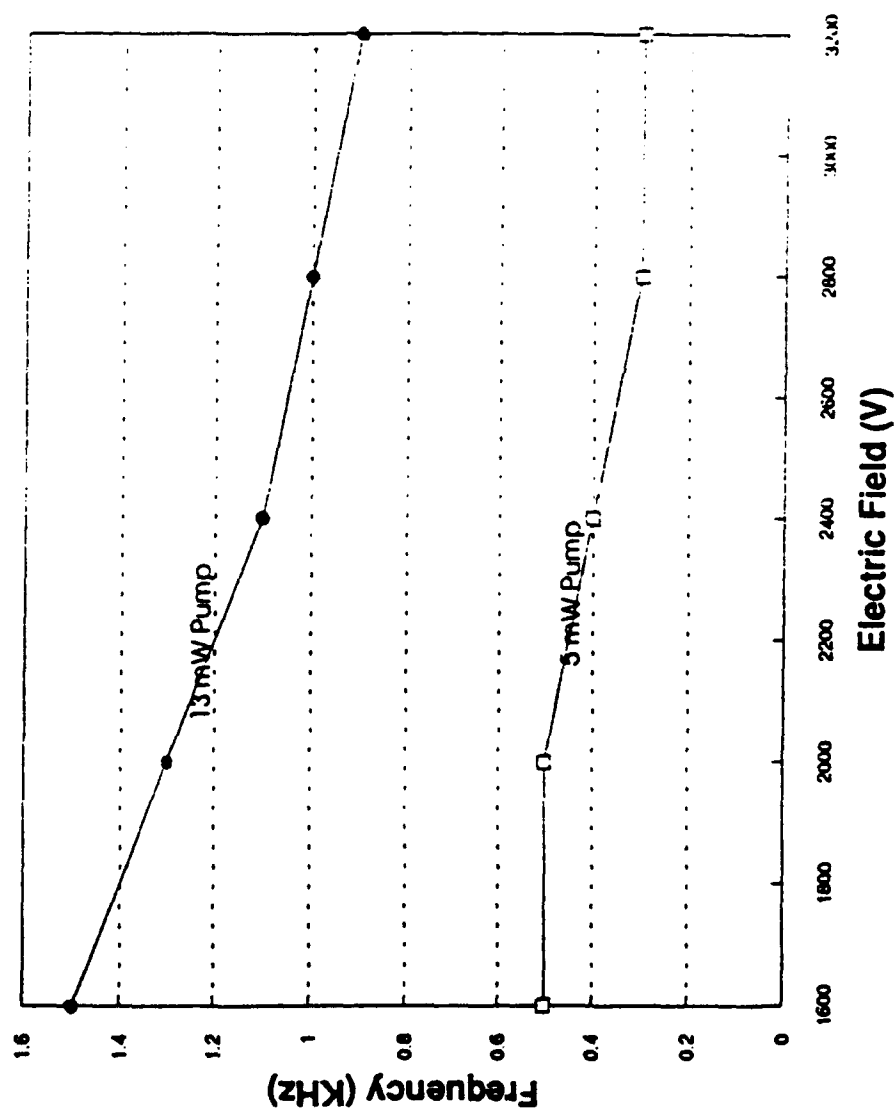
III-4 Effect of grating wavelength and pump intensity on bandwidth

Effect of Electric Field Strength on Detected Signal Level



III-5 Effect of electric field strength on detected signal level

Effect of Electric Field Strength on Resonant Frequency



relates to the resonant velocity. Two curves plotted for two different pump intensities show similar responses.

Grating wavelength

The spatial frequency of the grating shows up in both the numerator and denominator of the space charge electric field equation in a form that implies an optimum value. This is a commonly characterized parameter in photorefractive materials. In or near saturation the K^2 term dominates the denominator and a net inverse relationship occurs between grating amplitude and spatial frequency. The resonant velocity likewise should increase as the grating wavelength increases. Figure III-7 shows the bandwidth of the resonance vs. grating wavelength for various pump intensities. The data shown here is a different representation of the data contained in Figure III-4. All curves show a general increase in bandwidth as the grating wavelength increases, with the higher pump intensities providing the most extreme change. Figure III-8 shows the resonant frequency as the grating wavelength increases. Three curves are shown representing different pump intensities.

Reference dependence

Figure III-9 illustrates the relationship of the reference light level for all other parameters held fixed. The direct detect level drops 6 dB for 6 dB drop in reference level. The heterodyne signal follows this same general trend, but illustrates a saturation at the higher reference level. At the upper reference level the beam ratio is 12.5/1. This saturation effect is illustrated in the model in the next section and is due to the fact that a small angle allows the diffraction efficiency to become large enough that the signal beam starts to deflect into the wrong path. This is discussed in more detail in the following section. Figure III-10 illustrates the experimental points (triangle and square) plotted against the model. The lower curve represents the upper trace on Figure III-9 with the smallest pump to reference beam ratio. An independent measurement determined the gain coefficient to be 1.5 cm^{-1} under similar conditions of illumination.

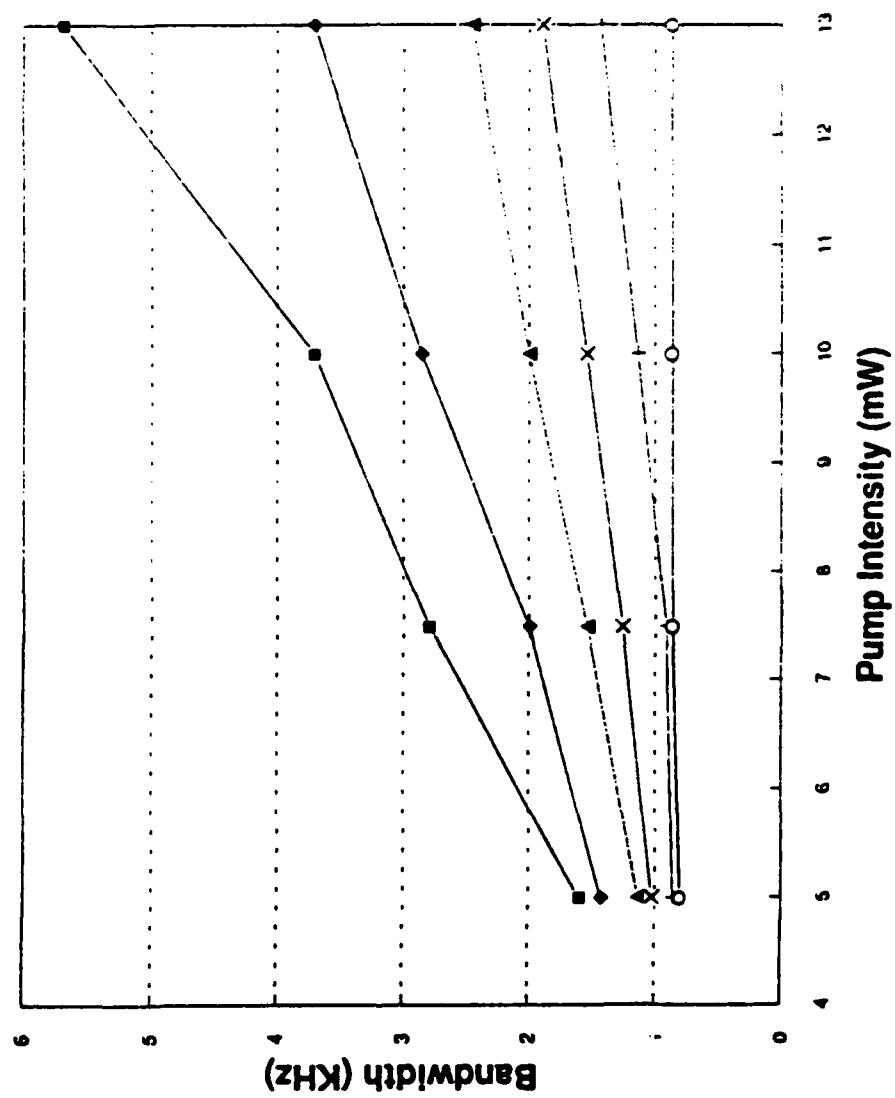
Signal dependence

The signal level dependence in Figure III-11 follows the general trend of the model predictions in that it is a dB for dB dependence. The heterodyne signal follows this dependence quite well. The direct detect level shows an apparent compression at the low signal end. The low end measurement is limited by detector noise.

Signal and reference dependence

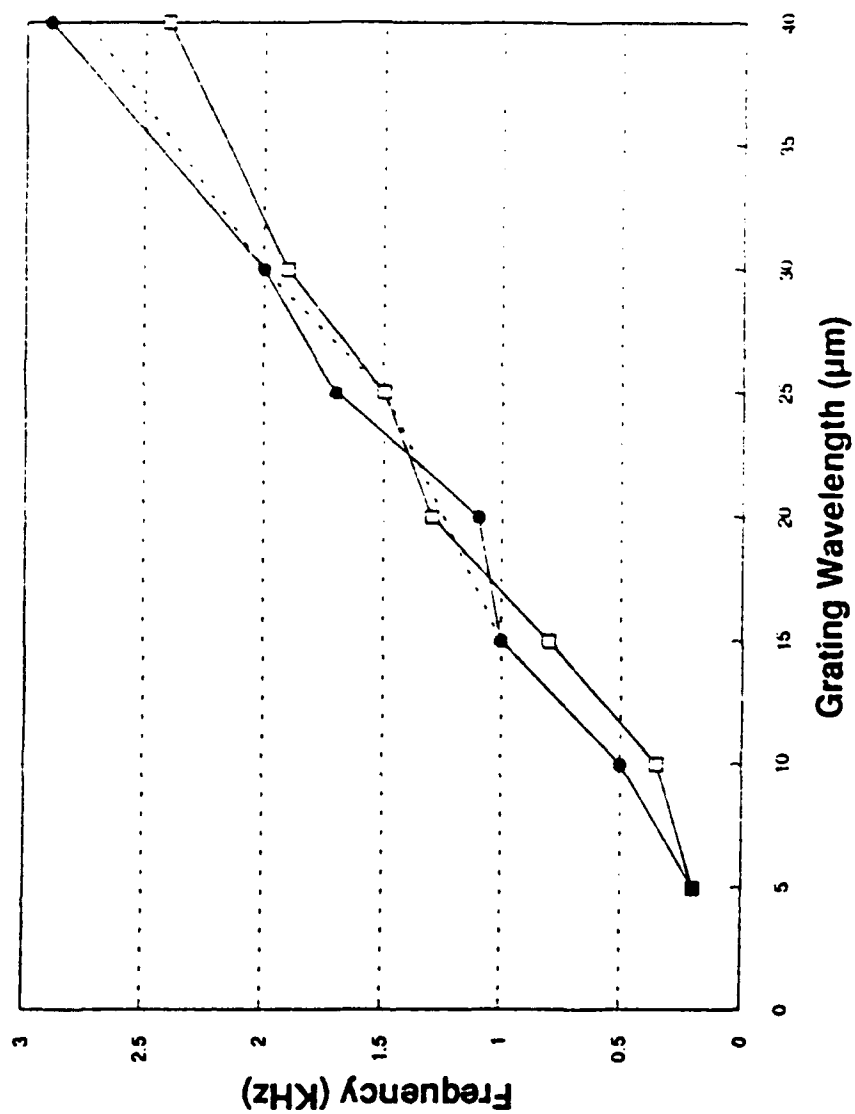
As one might expect when the received light is reduced, that is the signal and the reference component, the detector output falls 2 dB for every dB loss in the received light.

Effect of Pump Intensity and Grating Wavelength on Bandwidth



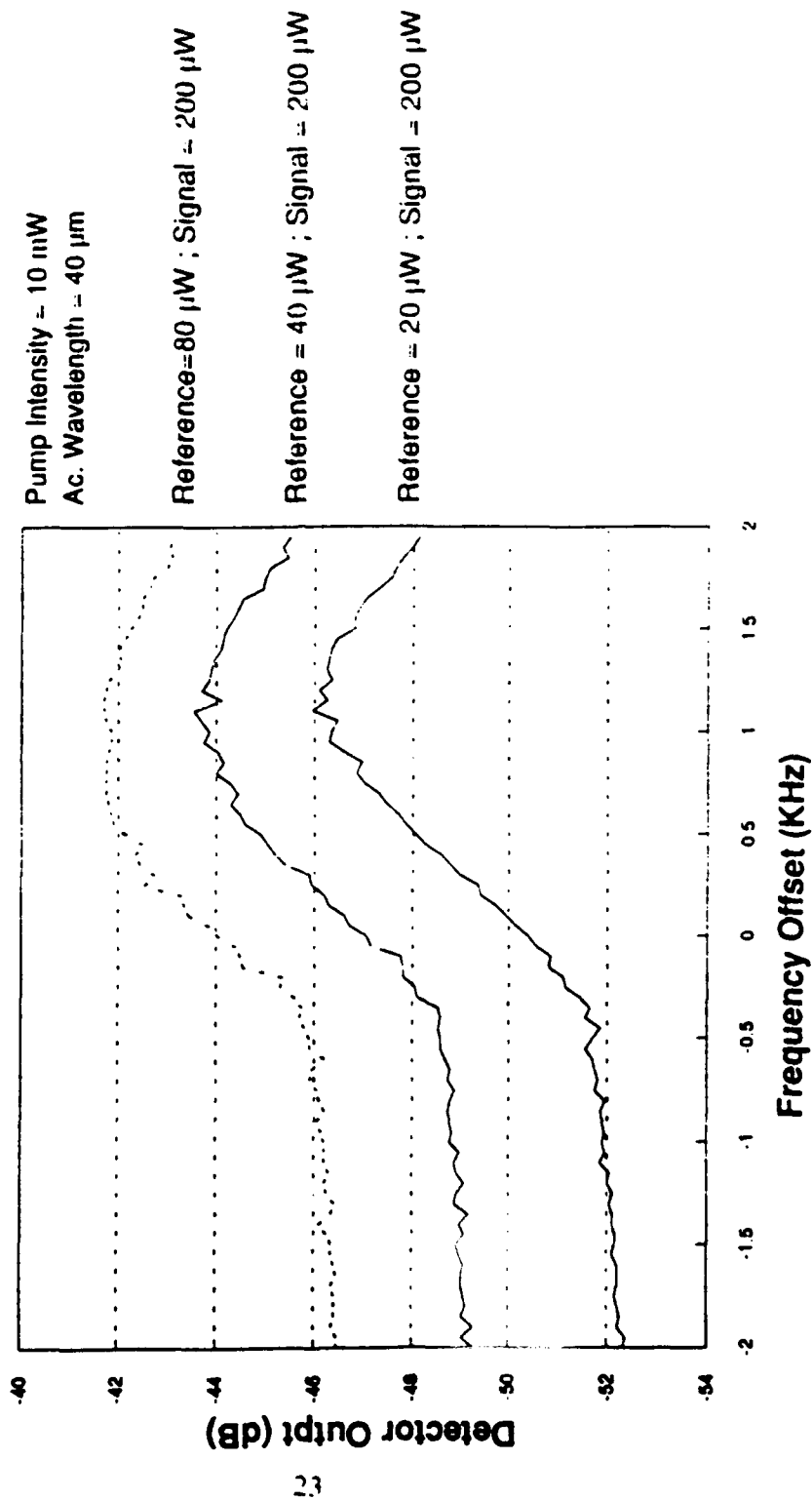
III-7 Effect of pump intensity and grating wavelength on bandwidth

Effect of Grating wavelength on Peak Resonant Frequency



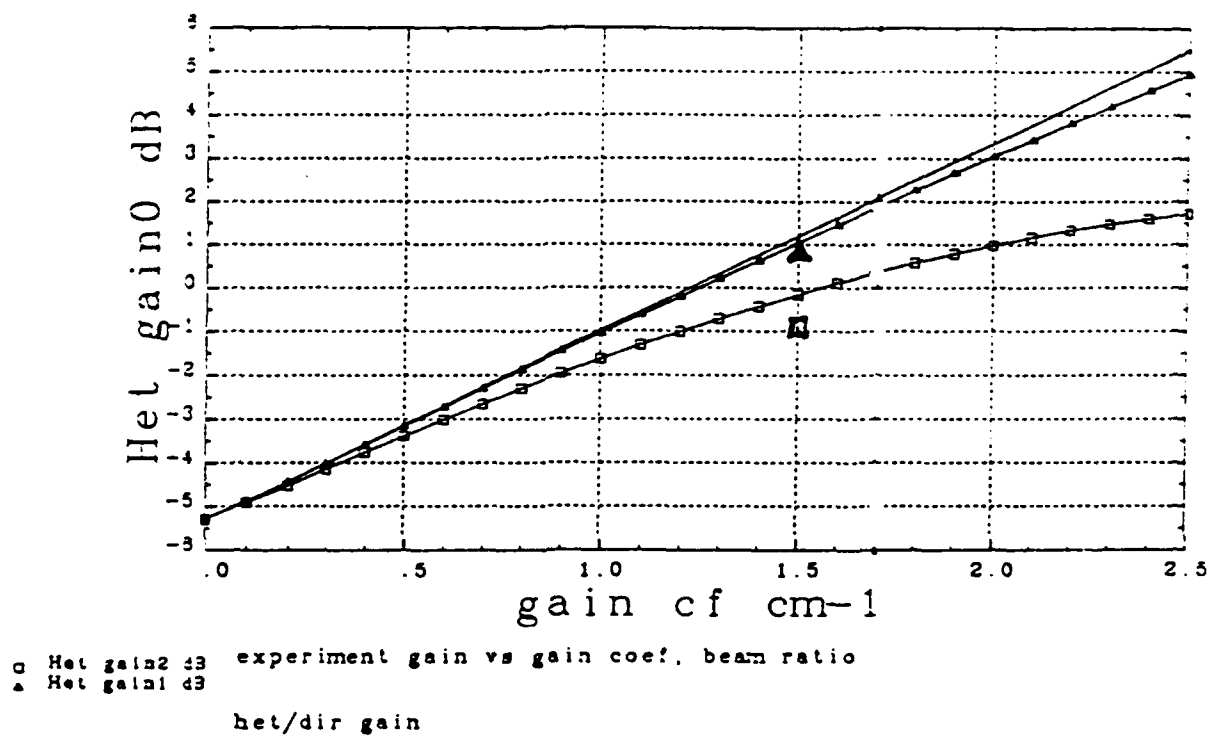
III-8 Effect of grating wavelength on peak resonant frequency

Effect of Reference Intensity on Resonant Amplitude and Bandwidth



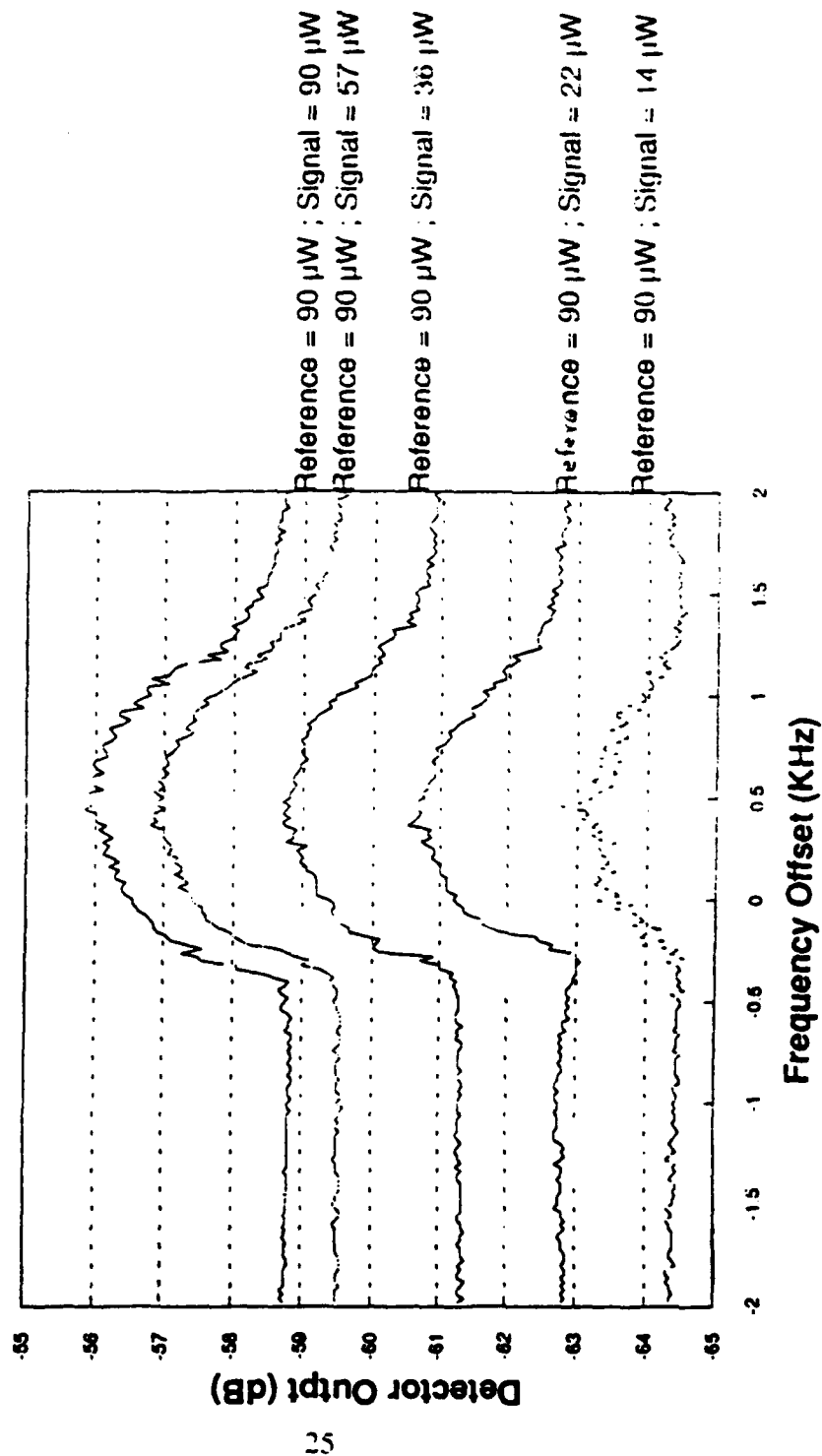
III-9 Effect of reference intensity on resonant amplitude and bandwidth

Experimental comparison with Heterodyne Gain



III-10 Experimental comparison with heterodyne gain

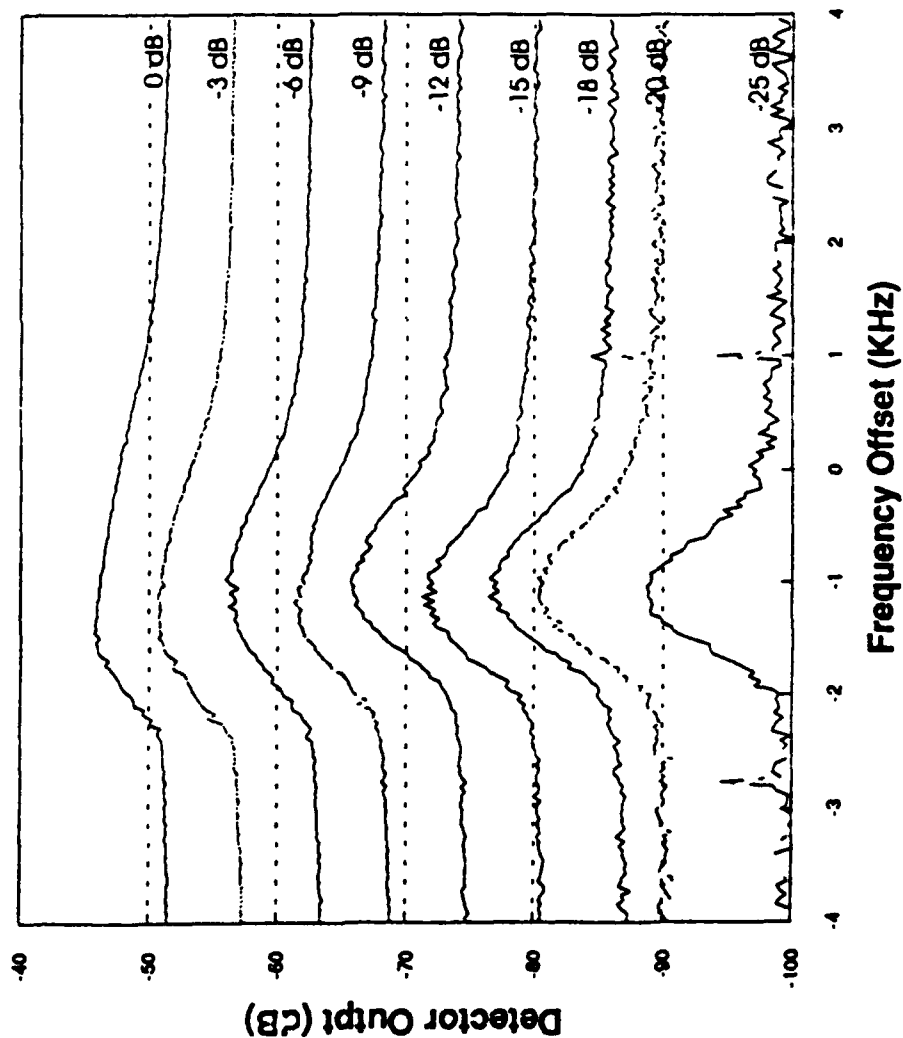
Effect of Signal Intensity on Resonant Bandwidth and Amplitude



III-11 Effect of signal intensity on resonant bandwidth and amplitude

Effect of Beam Ratio on Amplitude and Bandwidth

Reference Intensity = 100 μ W @ 0 dB
 Signal Intensity = 100 μ W @ 0 dB
 Pump Intensity = 13 mW
 Ac. Wavelength = 40 μ m



III-12 Effect of beam ratio on amplitude and bandwidth

The data in Figure III-12 shows 50 dB reduction in detector signal for 25 dB reduction in input beam power. This is as the model of Section IV predicts. Notice the bandwidth broadening at the upper light levels where the incident beam contributes significantly to the photoconductivity. It should be noted that there is a 10x demagnification of the signal and reference so that the 200 microWatts of power corresponds to a 15% light level increase on the photorefractive material.

Absorption coefficient

The absorption coefficient partly manifests itself in the governing equations through the Maxwell relaxation time, τ_M . Absorption contributes to photoconductivity in that a percentage of photons absorbed contribute to the photoconductivity (hopefully most of them). The rate of photoelectron generation is approximately given by,

$$(11) \quad \frac{dn}{dt} = \frac{\alpha I \eta_q}{h\nu}$$

where α is the optical power absorption coefficient, I is the optical intensity and η_q is the photoelectron quantum efficiency.

We therefore expect to see trends related to absorption similar to pump intensity. The resonant velocity, inversely related to τ_M , should increase as the absorption increases, and the bandwidth should increase as well. Figure III-13 is a plot of two curves taken with the same parameters, but different crystal samples. The absorption coefficient at 1.06 microns of the lower trace is 2.9 cm^{-1} , while the upper trace is 0.62 cm^{-1} .

Vibration correction

The compensation of system instabilities, such as platform vibration or dynamic atmospheric aberration, is one of the photorefractive processes most advantageous properties. The dynamic grating formed in the crystal automatically corrects for wavefront differences between the pump and reference beams. The speed at which the grating can adjust is measured by the material response time, τ_{sc} , and thus directly affected by the bandwidth of the signal vs. velocity resonance peak. We would therefore expect to see vibration insensitivity at higher frequencies for broad bandwidth resonance. The material measured in this study had a minimum measured bandwidth of 700 Hz and a maximum bandwidth of 5 KHz.

Vibration was simulated in the test setup by placing a piezo translator on one of the folding mirrors in the reference and signal path and driving it with a sinusoidal signal to

create a vibrational movement on the mirror. The high voltage amplifier that drove the piezo had a peak drive frequency of about 600 Hz before it began creating large amounts of harmonics in the drive signal. Measurements above this frequency were not considered well established due to the higher harmonic components.

The Figure III-14(a) shows a frequency scan as described previously of the material sample with no vibration in the system. From the curve we can measure a 3 dB bandwidth of approximately 800 MHz. The vibration was then added into the system at increasing frequencies, while the peak signal intensity was recorded for each frequency. Figure III-14(b) shows the results. Although we could not measure out to the full 3 dB bandwidth with our setup, we can demonstrate that only a small amount of signal strength is lost due to vibrations up to 600 Hz. This corresponded well to the frequency scanned measurements for the same experimental conditions of minimum bandwidth. Thus, predictions out to 4 kHz from the frequency scan should be valid.

Experiment summary

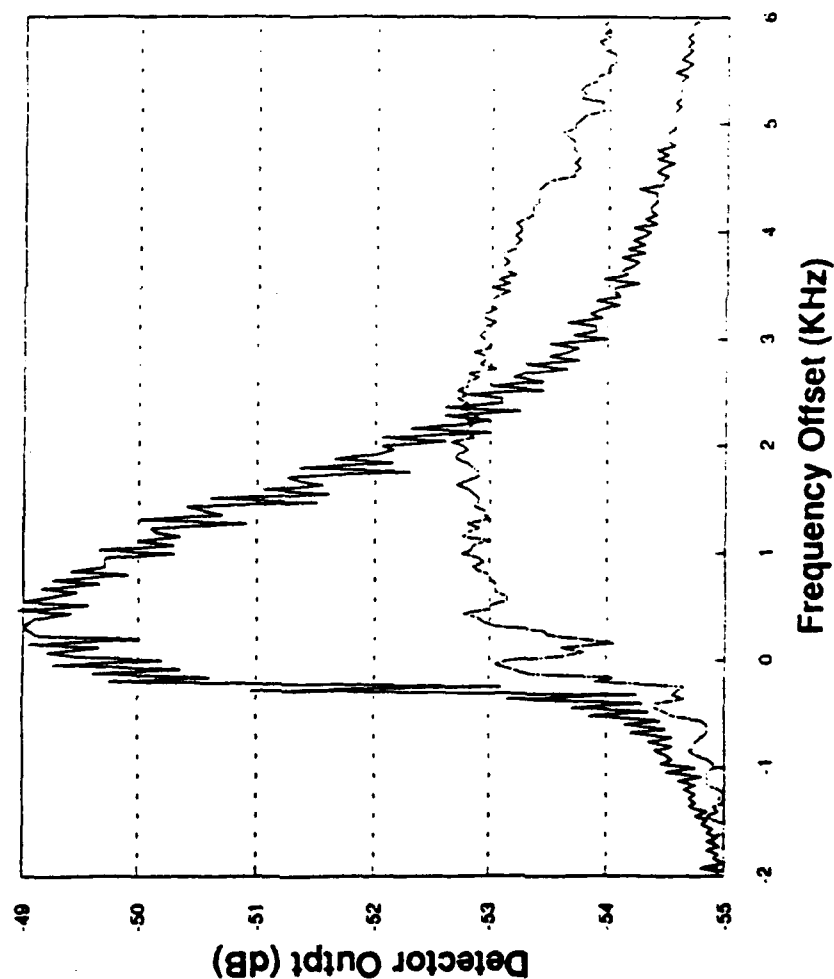
We have discussed the effects of varying many individual parameters on the grating amplitude, bandwidth and resonant velocity. These effects can be optimized for a system's particular requirements, and in many cases require a trade analysis between several opposing characteristics. The primary characteristics are adequately described by the single carrier model for the particular experimental parameters used here. Several key points are listed here as summary to the experimental results.

The pump intensity primarily affects the time response of the grating formed in the photorefractive cell. In most applications the reference power will be weak. The optimum pump power is dependent on the need for vibration and aberration correction in a homodyne system, and additionally on the independent laser linewidths in a heterodyne receiver with independent laser sources. Increased pump power does not offer the advantage of increased signal level as it does in utilizing a conventional beam combiner. This is a major shortcoming and is discussed further in the following section.

The optical design of the photorefractive system should optimize the angle between the pump and reference beams at the photorefractive crystal, determined by the bandwidth required and the gain of the photorefractive system needed. The gain of the system is only weakly dependent on the beam angles, and thus broad band in an angular sense.

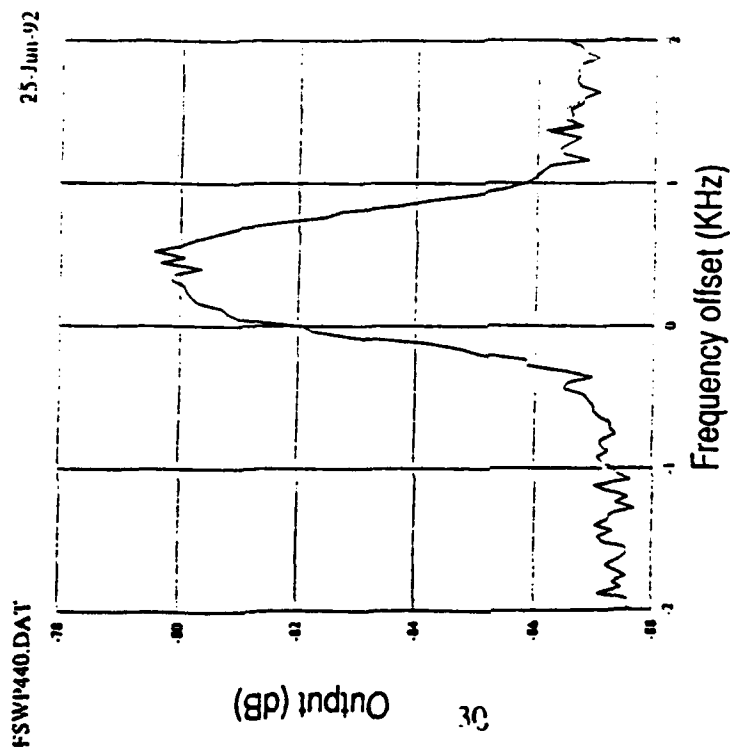
We utilized two modulation methods with the experimental setup. A simple single sideband modulation with sideband of equal or less strength compared to the carrier intensity and a carrier suppressed single sideband modulation scheme where the carrier was of less intensity than the sideband were simulated by varying the relative intensities of the reference and signal beams. Double sideband modulation was not considered, but results may be extrapolated from the single sideband modulation results. As one might expect, the gain of the system is not a function of signal intensity since this beam is "incoherent" with the other

Effect of Material Properties on Resonant Amplitude and Bandwidth



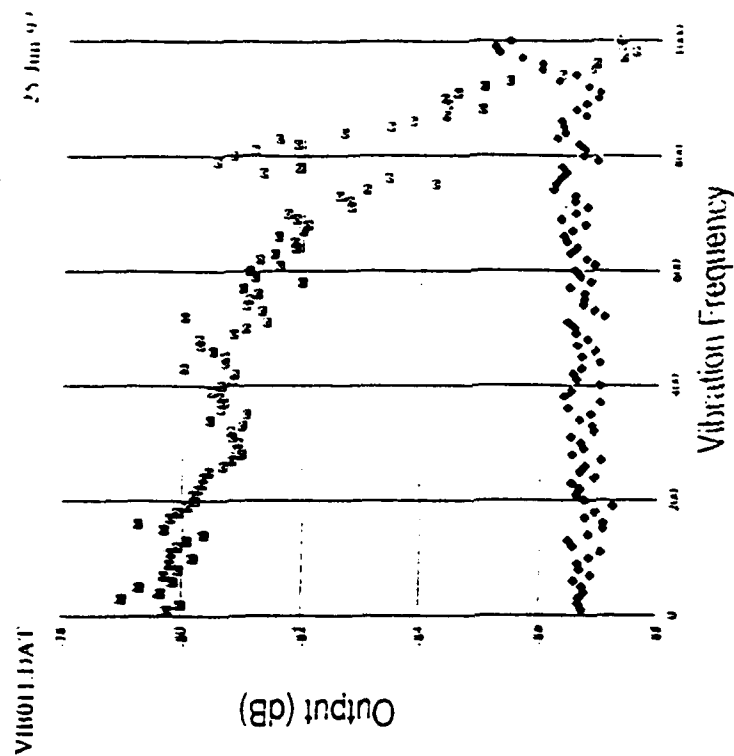
III-13 Effect of material attenuation on resonant amplitude and bandwidth

Detector Output vs. Frequency Offset



Signal Frequency Scan

Detector Output vs. Vibration frequency



Vibration Frequency Scan

$\lambda = 20 \mu\text{m}$
 Reference Intensity $\approx 1 \mu\text{W}$
 Signal Intensity $\approx 1 \mu\text{W}$
 Pump Intensity $\approx 10 \text{ mW}$

two beams in the sense that it does not contribute to the formation of the photorefractive grating. The signal beam does however contribute to the incoherent erasure of the grating, and may impact the performance of the system if made too large. The grating strength is a function of the reference intensity, in the form of the pump and reference intensity beam ratio.

IV. Heterodyne Gain

There have been several good papers^{[Bylmas],[Hamel de Monchenault],[Dolfi],[Davidson]} on the utilization of a photorefractive beam combiner for homodyne/heterodyne signal reception. They have illustrated without doubt that the photorefractive beam combiner works in the sense that signal magnitude can be increased by wavefront matched combination of the incident signal with a larger local oscillator. These works illustrate differential gain of the incident signal and derive relationships to express the gain in terms of photorefractive gain. Application to both digital and analog modulation are shown. Dolfi et. al., discussed the issue of signal-to-noise performance. In the case of Davidson et. al., calculations and measurements of Bit Error Rate are made for optimum modulation schemes and compared to more conventional optical receiver techniques.

This current work investigates the requirements on the photorefractive beam combiner, in a general receiver process, for various systems applicability. In particular concentration is placed on the development of simple relationships to perform parameter trades. The issues of interest are heterodyne gain, signal-to-noise ratio (SNR), photorefractive gain and photorefractive bandwidth. These parameters are discussed in terms of their interrelationships.

Heterodyne gain refers to the signal gain due to heterodyne detection of the signal. This is quite apart from photorefractive gain, which is a property of the photorefractive interaction. Heterodyne gain is perhaps the more appropriate perspective for discussion of heterodyne receivers since it is a system parameter of interest.

Heterodyne gain can occur independent of photorefractive gain. A half coated mirror utilized as a beam combiner will provide heterodyne gain on a photodetector, as will a photorefractive material that has the wrong phase relationship to exhibit photorefractive gain. Photorefractive gain is required, however, for a photorefractive heterodyne receiver system to offer a significant amount of heterodyne gain.

Photorefractive diffraction efficiency is limited to four times the ratio M_0 of the weak incident reference beam to the strong pump beam for the case in which there is no photorefractive gain, as illustrated in the well known Equation (12)^[Kukharov]. In an optical heterodyne receiver this beam ratio is necessarily very small (if not, there is little need for a heterodyne receiver). Diffraction efficiency must necessarily be significantly larger than this limit to offer optimum heterodyne signal gain. It must typically be tens of percent to

optimize the receiver by diffracting the largest possible local oscillator pump onto the photodetector with minimal loss of the signal. This level of diffraction efficiency can be achieved via the exponential growth in the diffraction grating strength produced under gain conditions. The diffraction efficiency, in the case of gain, can approach 100% as illustrated in Equation (13)^[Kukharov]. Thus, photorefractive gain is required for small beam ratios to produce significant diffraction coupling efficiencies.

$$\eta = 4 \frac{M_o}{(1-M_o)^2} \sin^2(\gamma L/2) \quad (12)$$

$$\eta = \frac{M_o(e^{\gamma L/2} - 1)^2}{(1+M_o)(1+M_o e^{\gamma L})} \quad (13)$$

An experimental measurement of heterodyne gain may be done by a direct comparison of the heterodyne signal, when the photorefractive material is active, to the direct detected signal, when the material is not active (when the pump is blocked). This method of conducting the experiments adds the photorefractive attenuation on top of the direct detect signal, so that for a fair comparison the signal attenuated due to the photorefractive material must be added back on to the direct detect component. That is, the photorefractive material would not be in the light path in a direct detect system, whereas it is in the light path for the heterodyne system. The analysis below presents heterodyne gain as the heterodyne signal detected, compared with the direct signal without attenuation.

In addition to heterodyne gain, a significant parameter of interest, from a systems point of view, is the Signal-to-Noise-Ratio (SNR) of the receiver. In the context of a photorefractive heterodyne receiver the important merit parameter would be the ratio of the heterodyne SNR to the direct detect SNR. Ideally, a receiver system would be shot noise limited in order to maximize the dynamic range. Note that the ratio of signals alone (heterodyne gain) is equal to the SNR ratio when the heterodyne signal and the direct detect signal have a common receiver noise floor, such as thermal noise.

Heterodyne gain model

Some simple relationships can be developed which illustrate the dependence of heterodyne gain on incident light and material parameters in various limits. The relationships consist of a ratio of the heterodyne signal-to-noise level to the direct detect level, in various noise limits. The model of the problem consists of light incident on the photorefractive material comprised of a pump beam and a low level reference beam that has a modulated signal component. The pump beam and the reference are coherent or nearly coherent (within the response time of the photorefractive material) with each other and the signal component is offset in frequency (outside of the material response time).

The signal may be generated by amplitude modulation of the reference, frequency modulation or addition of a separate beam at an offset frequency (single sideband modulation). The pump and the reference are actually responsible for the generation of the photorefractive grating. Figure IV-1 illustrates the point that regardless of the modulation technique, the unmodulated carrier component can act as the reference. For example, amplitude modulation consists of a dc component with double sidebands of relative magnitude $m/2$ each. It is the unmodulated dc component which may be used to interfere with the pump in the photorefractive material to form the grating, while the modulated sidebands simply deflect off of the grating to interfere with the pump on the photodetector. This is illustrated in Figure IV-2, which shows the general receiver concept, where S_0 is the unmodulated component and $S(t)$ is the temporally modulated part. It is, thus, no great surprise that one can form a photorefractive grating independent of modulation frequency.

A heterodyne signal current is generated on the photodetector when the pump and signal are combine via the photorefractive grating formed by the pump and reference. This current signal has the form,

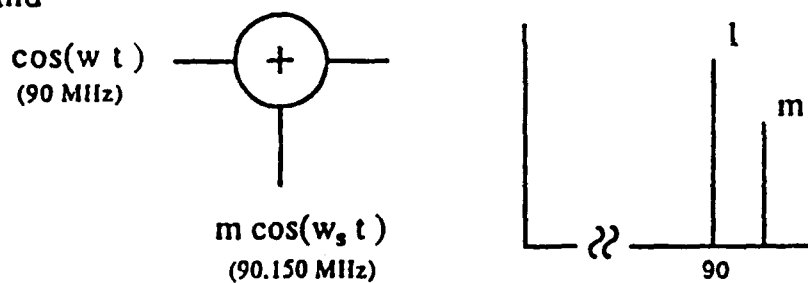
$$i_{sig} = \Re A(mS^2 + PSm\sqrt{\eta})\sqrt{1-\eta}e^{-\alpha L} \quad (14)$$

This can be compared to the direct detected signal which is observed if the photorefractive element is not present,

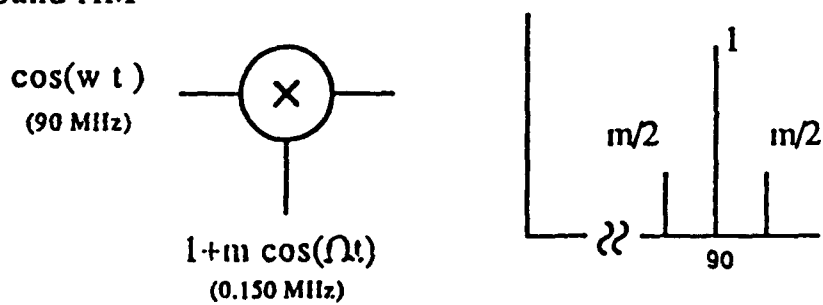
$$i_{sig} = \Re A m S^2 \quad (15)$$

MODULATION TECHNIQUES

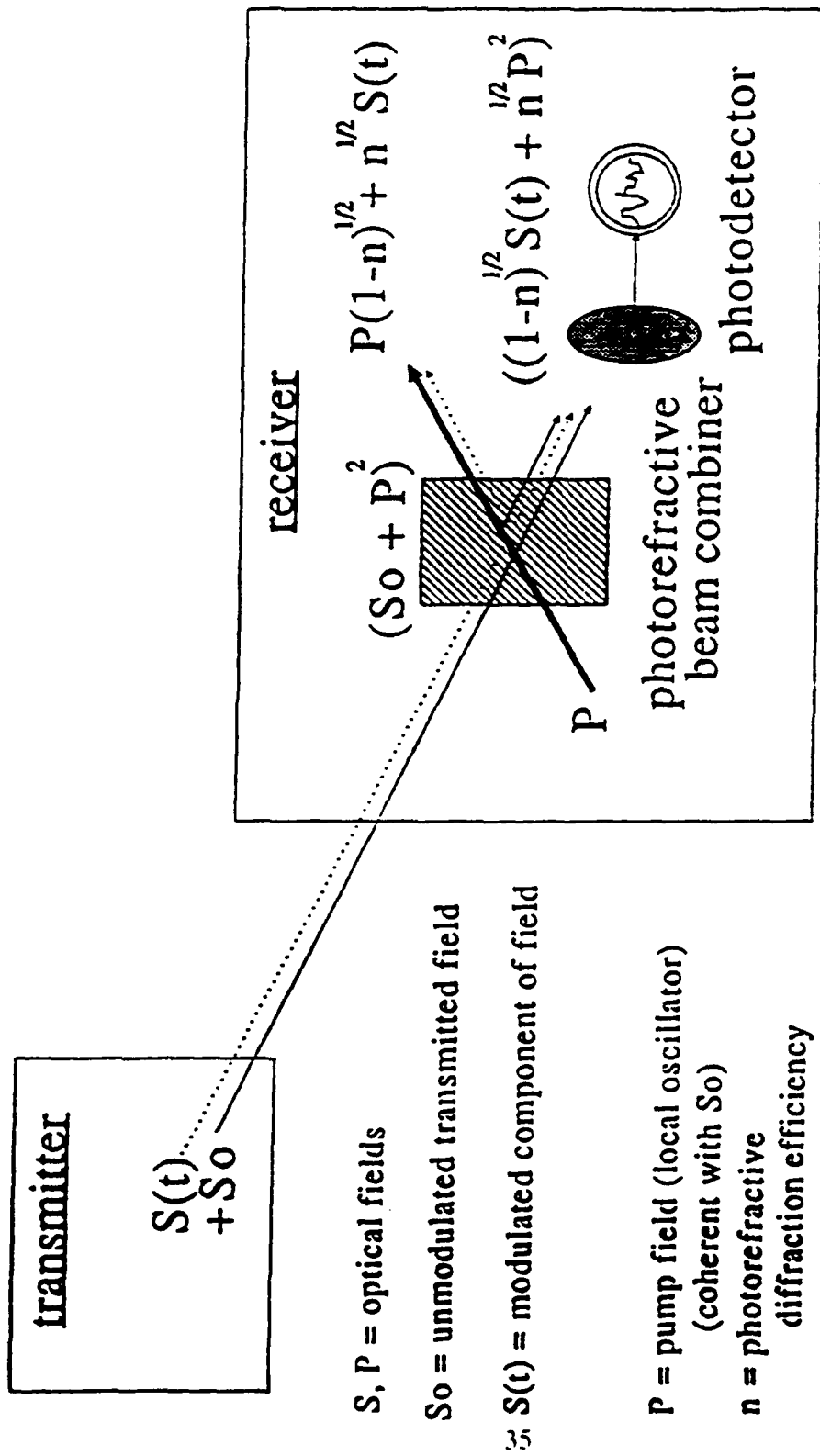
Single sideband



Double sideband AM



IV-1 Modulation techniques



S, P = optical fields

S_0 = unmodulated transmitted field

$S(t)$ = modulated component of field

P = pump field (local oscillator)
(coherent with S_0)

n = photorefractive
diffraction efficiency

Here, \mathcal{RA} is the usual detector responsivity $e\eta/(h\nu)$ times the area and m is the modulation ratio. It represents the ratio of the modulated field component to the unmodulated dc (reference) field. S is the reference field, and P is the pump field. η is the light diffraction efficiency and α is the optical attenuation coefficient, with L being the optical interaction length.

A ratio of these signals in terms of photodetector current is given by,

$$\frac{Sig_{het}}{Sig_{dr}} = [1 + \sqrt{\frac{\eta}{M_0}}] \sqrt{(1-\eta)} e^{-\alpha L} \quad (16)$$

where M_0 is the ratio of the reference light intensity to the pump intensity. Note that this relationship corresponds to the ratio of heterodyne to direct SNR when detection is dominated by $4K_B T B/R$ noise, the usual thermal noise. It is easily seen that for a system to have a heterodyne gain greater than 1,

$$\frac{e^{\alpha L}}{\sqrt{(1-\eta)}} - 1 < \sqrt{\frac{\eta}{\beta}} \quad (17)$$

which requires that the photorefractive gain coefficient must exceed the attenuation coefficient by more than a factor of two. In particular,

$$\Gamma > 2(\alpha - \frac{\ln(\sqrt{1-\eta})}{L})$$

A similar relationship can be derived for the ratio of heterodyne SNR to direct detect SNR in the shot noise limit. This relationship gives further insight into the trade-off of receiver parameters. This relationship is found to be,

$$\frac{SNR_{het}}{SNR_{dir}} = \left(1 + \sqrt{\frac{\eta}{\beta}} \sqrt{1-\eta} e^{-\alpha/2}\right) \delta \quad (19)$$

where

$$\delta = \sqrt{\frac{1/2(1-m^2)}{\gamma}} e^{\frac{\alpha L}{2}} \quad (20)$$

and

$$\gamma = \frac{1}{2} \frac{\eta}{\beta} + \sqrt{\frac{\eta}{\beta} + \frac{1}{2}(1+m^2(1-\eta))} \quad (21)$$

These additional terms result from the shot noise component of the beams.

Relation (19) provides interesting insight into the interrelationship of the light levels, modulation depth and diffraction efficiency, but it is not a very practical limit. If the direct detect component were shot noise limited there would be no need for heterodyne detection. Ideally one should retain all of the relevant noise terms and optimize the system parameters to obtain shot noise limited performance of the heterodyne component. Although this approach is appropriate, it leads to more complicated relationships and requires specific assumptions about the system. The simpler relationships above illustrate the relevant trades without requiring specific assumptions about the detector.

In general, the dominant noise terms at signal frequencies are thermal and shot noise. An approximation to the RMS noise current within a given bandwidth is shown in Equation (22).

$$i_{\text{noise}} = \sqrt{\frac{4K_B T \Delta f}{R} + 2e \Delta f \Re A \left[\eta \frac{P^2}{2} - \sqrt{\eta} P S - \frac{S^2}{2} (1 - m^2 (1 - \eta)) \right] e^{-\alpha L}} \quad (22)$$

The noise current terms illustrated here are the thermal noise and the shot noise terms. The photorefractive noise (beam fanning) and other potential noise terms are assumed small, but could be added as required. Note that the attenuation affects shot noise as the square root of the exponential whereas it affects the signal as the exponential.

The implications of these relationships (16 - 19) are quite interesting. Equation (17) illustrates that the attenuation can be the dominant term. The fact that attenuation is important is not surprising. It is clear from these relations, though, that the magnitude of the effect justifies special emphasis. η is proportional to $e^{\Gamma L}$ and the detected signal is proportional to the square root of η , so, as mentioned above, the gain must exceed the attenuation by a factor of two before a positive signal ratio exists. Comparison to experimental data from the literature^(Table IV-1) illustrates this point quite well.

Two particularly interesting cases are the data of Ozkul et. al., and Partovi et. al. The data of Partovi et. al. is the highest gain coefficient measured to date in gallium arsenide as a photorefractive material. The data of Partovi et. al. utilizes a short wavelength to obtain band edge gain enhancement, and the Ozkul et. al. data utilizes a long wavelength to avoid high attenuation, as does the data of Bylsma et. al. None of the experiments at 1.064 micron YAG wavelengths illustrate significant heterodyne gain performance. The relevant parameters are listed in the following table.

Table IV-1. Gain Comparison

Material	Gain Coeff. cm ⁻¹	Tot. Gain	Atten. cm ⁻¹	Beam Ratio	Het. gain dB
GaAs ^(Partovi)	16.3	600	3	1/4830	14
InP ^(Ozkul)	6.5	100	2.6	1/8000	3
InP ^(Ozkul)	5.3	45	0.5	1/700	13
InP ^(Mainguest)	4	5	2	1/80	0
InP ^(Bylsma)	2.5	10	0.15	1/50	8

The calculated heterodyne gain implied from Equation (16) is listed in the last column of the table for all of the experiments. Note that only authors of the last experiment in the table actually injected signal into the system for measurement, so the results are calculated based on the assumption that the addition of the modulated component does not affect the above measurements. The signal component would have the effect of background light since its frequency offset is outside of the response of the material. This component is typically small compared to the pump beam, however, and should not be significant.

Note that the highest gain coefficient provides the highest total gain, and with relatively little loss. This crystal provides the highest heterodyne gain. The second case illustrates twice the gain of the third case and an order of magnitude higher total gain than the fifth, but 10 dB and 5 dB less heterodyne gain, respectively. The fourth case demonstrates no heterodyne gain at all. This clearly illustrates the sensitivity to optical attenuation. These results follow directly from Equation (17). Another way of looking at this is to say that heterodyne gain is proportional to the pump field incident on the detector while loss affects the combined power since both the pump and signal beam are attenuated.

The curves shown in Figure IV-3 illustrates the signal ratio of heterodyne to direct detect. The curves are plotted against gain coefficient Γ . Γ is related to η via the Equation (13). The reference/pump beam ratio M_0 is shown, three different values, on the curves. The parameters used in Figure IV-3 are from the first experiment^(Partovi) in Table IV-1, where the curves terminate on the maximum gain coefficient achieved in the experiment. Figure IV-4 illustrates the thermal noise and shot noise limit in the same experiment for an assumed 1 MHz receiver bandwidth at room temperature. This curve illustrates that there is no advantage of additional gain once the shot noise limit is achieved.

The curves of Figure IV-3 illustrate a diffraction depletion effect versus beam ratio. At small beam ratios a large diffraction efficiency is achieved at moderate gain coefficients and the heterodyne gain decreases with increased gain coefficient. More diffraction efficiency merely serves to steal the signal beam from the receiver path, as illustrated in Equation (16). For beam ratios less than an M_0 of approximately 10^{-3} , no further significant signal gain is realized at a given gain coefficient. That is, heterodyne gain is independent of pump beam intensity for small beam ratios. This point is also illustrated in Equation (16) by noting that diffraction efficiency η is proportional to M_0 in the small diffraction limit.

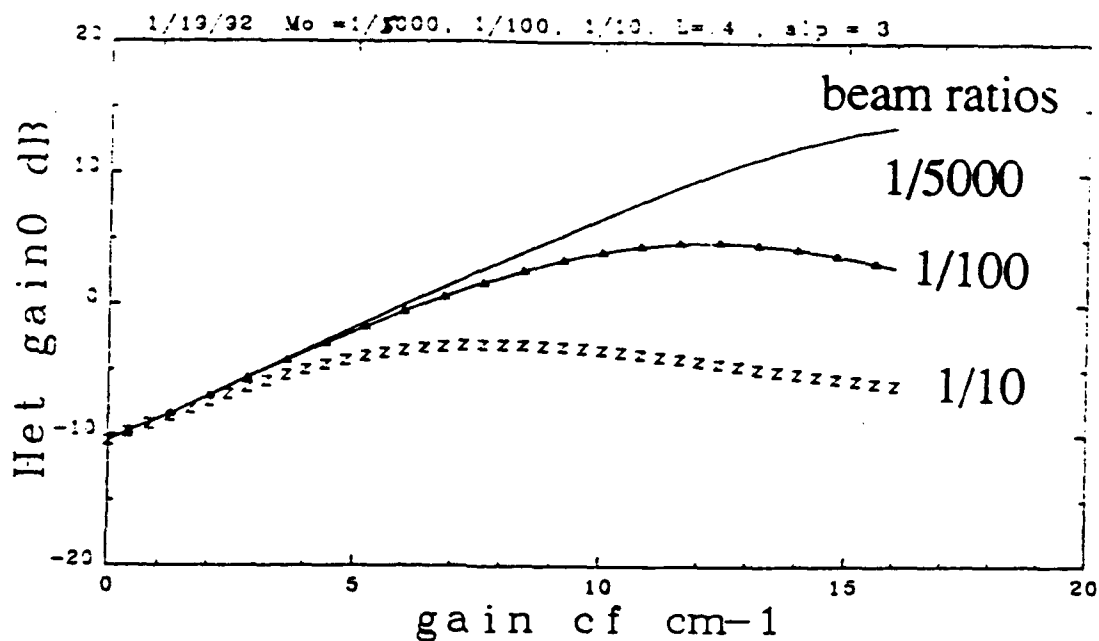
Figure IV-5 illustrates the same parameters plotted in terms of the shot noise limited performance, Equation (19). These curves further illustrate the point that if enough signal exists for the direct detection to be shot noise limited, there can be no advantage to heterodyne signal detection. The signal-to-noise is degraded by the heterodyne process even though there may be significant differential signal gain.

Photorefractive gain and gain-bandwidth

Photorefractive gain is generated when the preliminary photorefractive grating forming maintains a specific phase relationship to the incident light. There are many clever ways to obtain this relationship which has been investigated by many authors (see Table II-1). The gain, ultimately is a function of the material properties and the conditions of illumination. Maximum gain in the traditional photorefractive effect requires techniques to produce the maximum charge separation at a given spatial frequency with small initial light modulation depth by utilizing constructive feedback in the diffracted light interference. Optimum material coefficients produce larger gain coefficients. These include; as large of optical index and electro-optic coefficient as possible, and as small a dielectric coefficient as possible. This

Heterodyne Gain

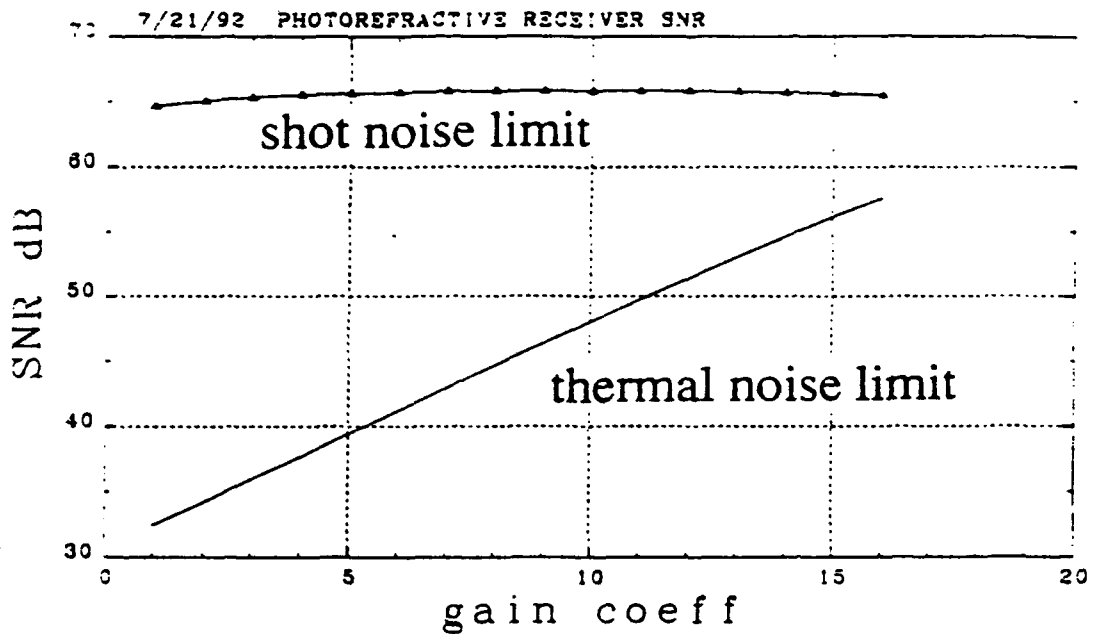
$$\text{Gain} = 20\text{Log}[\text{Heterodyne Signal} / \text{Direct Signal}]$$



variation with gain coeff
 ▲ Het gain: dB
 het/dir gain 3

IV-3 Heterodyne gain

Heterodyne SNR



▲ SNR shotdB

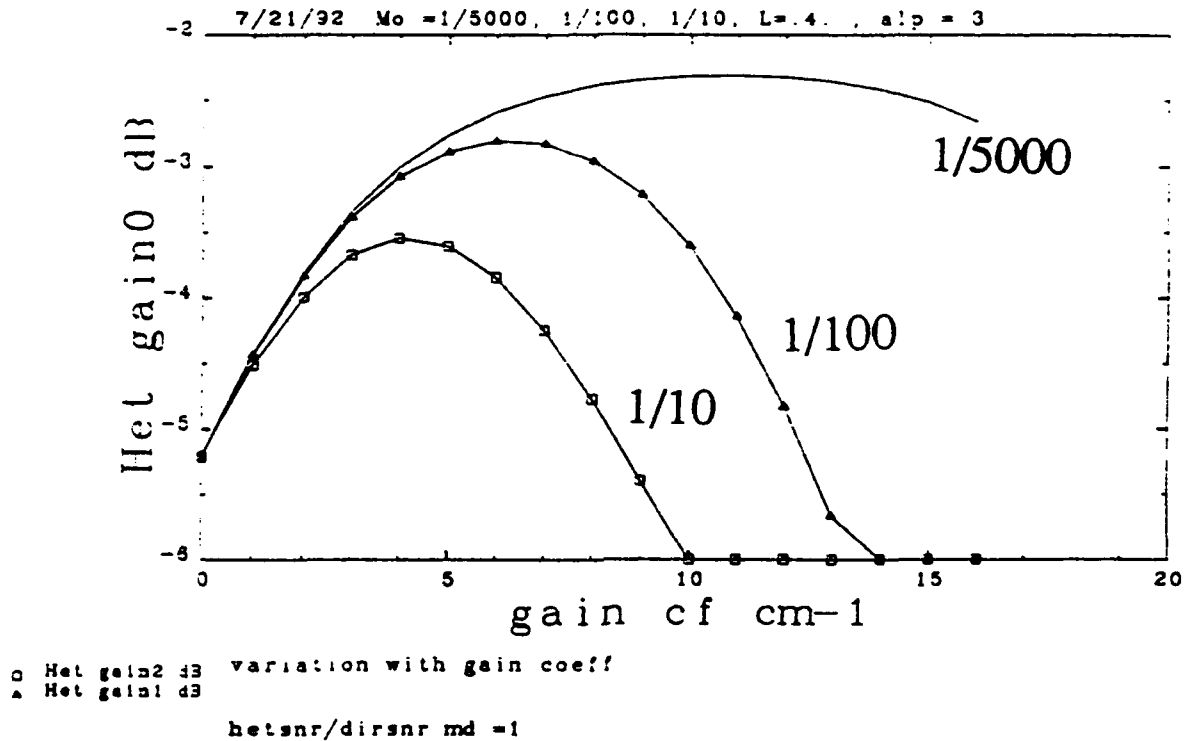
variation with gain coeff

$M_0 = 1/5e3$ $L = .4$ $\alpha_{lp} = 3$ $m_d = 1$ $T = 300$ K $B = 1$ MHz $P_0 = 13$ mW

IV-4 Heterodyne SNR

Heterodyne SNR Gain

$$\text{Gain} = 20\text{Log}[\text{Heterodyne SNR} / \text{Direct SNR}]$$



IV-5 Heterodyne gain, shot noise limited

is seen from the fact that the space charge field that forms is proportional to the charge density ρ reduced by the dielectric coefficient and the spatial frequency, or

$$E_x \propto \frac{\rho}{eK} \quad (23)$$

When substituted into Equation (i) for the diffraction efficiency the basic material parameters contributing to gain become apparent.

The charge density modulation that can be created and maintained is the key parameter that involves the charge dynamic properties of the material. The rate at which a given charge density distribution can be created limits the time response of the material. Gain and time response are competitive processes as illustrated by^[7a],

$$\tau = \left(\frac{h\nu}{e}\right) \left(\frac{\lambda}{\Lambda}\right) \left(\frac{\Gamma}{\alpha}\right) \left(\frac{2}{\pi \eta IQ}\right) \quad (24)$$

where $Q = n^3 r / \epsilon$ and n is the material optical index, r is the electro-optic coefficient and ϵ is the material dielectric coefficient. This relationship may be viewed in terms of a gain-bandwidth product, since time response bandwidth is inversely proportional to time response of the photorefractive grating. It is apparent from this that pump intensity can offset the gain in the response time of the material. That is, an increase in gain can be offset by an increase in pump intensity to maintain a given response bandwidth. This relationship holds until trap saturation, or some other saturation process, dominates. Some of the time responses estimated in Table II-1 are scaled from this relationship.

An ideal gain and bandwidth for a given application can be approximated based on the realization that a total gain on the order of the pump-to-reference beam ratio optimizes the signal received. The required photorefractive response bandwidth is on the order of the bandwidth required to acquire the signal (form the grating). Equation (23) can be written in the form,

$$\tau = \kappa \frac{\Gamma}{I} \quad (25)$$

where κ can be measured for a given material under known conditions and is nearly constant

over certain ranges of illumination.

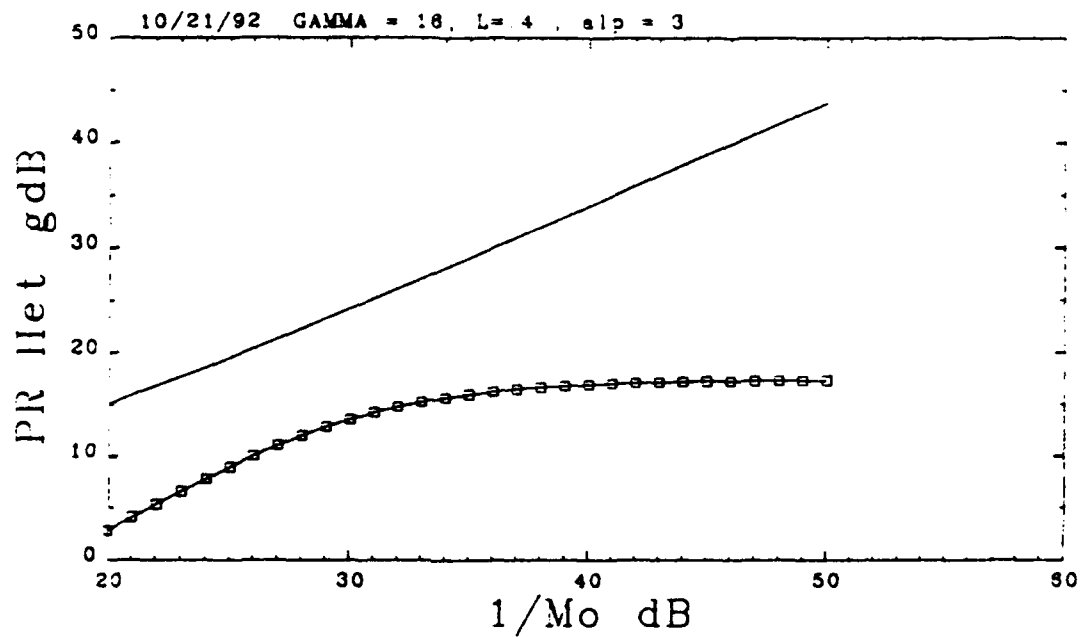
Given an incident signal level, the amount of pump required on the detector to obtain shot noise limited performance of the signal can be determined. Then a beam ratio of $\beta = I_{\text{pump}}/I_{\text{sig}}$ can be determined. The gain coefficient that must be achieved for optimum signal reception can be approximated for a given optical interaction length $\Gamma_{\text{opt}} \approx (\ln(\beta)/L)$. The pump intensity required to achieve the necessary response bandwidth is then determined from Equation (24).

Heterodyne pump dependencies

In comparison to a more traditional beam combining technique for an optical heterodyne receiver, a photorefractive beam combiner will probably have to provide sufficient gain to achieve shot noise limited performance to be competitive. A passive beam combiner with fixed reflectivity can always, in theory, put enough pump power on the detector to bring the signal to shot noise limit. For the traditional beam combiner, $\exp(-\alpha L)$ is essentially one and η is replaced by the beam combiner reflection. The pump can be increased arbitrarily, without affecting the reflectivity.

In the photorefractive case, the beam combiner deflection efficiency is given by, in the appropriate limit, $\eta = M_0 e^{\Gamma}$. Thus, as pump power is increased, diffraction efficiency is decreased, maintaining a fixed amount of pump power incident on the detector. This is illustrated in Figure IV-6, comparing a conventional fixed reflectivity beam combiner with a photorefractive beam combiner utilizing the parameters from the first experiment in Table IV-1. Note that 10 dB of pump power increase corresponds to 10 dB of detector signal for the conventional beam combiner, whereas the photorefractive beam combiner signal is independent of pump power once the beam ratio gets above the diffraction depletion limit. If insufficient photorefractive net gain exists under the conditions of the illumination, shot noise limited performance cannot be obtained by increase pump power.

The photorefractive beam combiner does offer the advantage of wavefront and jitter compensation. However, if the transmitter laser and local pump are several kHz line width lasers, the current state-of-the-art, that are frequency locked together, a kHz of mechanical vibration is inconsequential. In addition, the material response bandwidth would have to be greater than the correlated laser linewidths to develop a diffraction grating. If wavefront aberration is a problem on the incident light a smaller aperture can be sampled and mixed with larger local pump power utilizing a conventional beam combiner which is designed with optimum reflectivity. The photorefractive beam combiner might accept a larger, nondiffraction limited, aperture. But it would require one to help compensate for the optical losses. Thus, application of currently available photorefractive materials to a remote heterodyne receiver for the purpose of signal-to-noise gain does not appear to offer significant advantage.



□ at Het gdB variation with pump intensity

IV-6 Comparison of conventional to photorefractive beam combiners

An optical homodyne system, which utilizes the same laser as the reference and pump, may benefit from utilizing a photorefractive material as an adaptive beam combiner. For this case the laser linewidth only need be sufficiently narrow to account for spatial path differences between beams. Benefit is derived from the insensitivity to mechanical vibration within the response time of the material and insensitivity to alignment in addition to the insensitivity to quality of the optics. Furthermore, multiple beams can be combined simultaneously. Many other unique applications have been discussed for photorefractive elements as beam combiners including application to phase locking lasers, image processing and others (see references).

V. Conclusions and future potential

The results discussed above indicate that based on currently available materials utilization of a photorefractive adaptive beam combining element for heterodyne reception may be limited to a narrow range of special applications. The primary reasons for this may be stated simply as inadequate gain and inadequate response time of the available materials for many potential applications. The explanation is more involved.

From a systems perspective heterodyne gain is a key parameter of interest. Furthermore, heterodyne gain is only of benefit when the signal floor is limited by fixed receiver noise, such as thermal noise. The advantage of heterodyne gain is to bring the signal up out of the receiver noise, ideally, to its shot noise limit. Photorefractive gain must provide adequate diffraction efficiency at the system's required beam ratio to achieve significant signal gain after suffering the attenuation of the material. It must have adequate response time to accomodate frequency uncertainties between the signal carrier and the local pump.

In a conventional beam combiner heterodyne system the heterodyne gain is proportional to the local pump power. In a photorefractive beam combiner it is independent of local pump power. In terms of the beam combiner, for a fixed level of incident signal a conventional beam combiner inherently has a pump-to-signal diffraction gain proportional to the pump power (it has a fixed diffraction efficiency), the photorefractive gain is independent of pump power (its diffraction efficiency varies inversely as pump power). This is a problem if inadequate photorefractive gain exists at the required operating conditions. With measured photorefractive gains typically less than 100 few real receiver systems would derive benefit from a photorefractive beam combiner. This is particularly true when the optical attenuation required to form the diffraction grating is considered.

If an ideal photorefractive material were envisioned for this application it would have a response time adequate to develop a diffraction grating under conditions of the correlated laser linewidths of a transmitter laser and local pump laser or compensate for frequency offsets or platform jitter. The material must have adequate gain to compensate for twice the attenuation, just to break even, and it should have sufficient gain to allow the local oscillator to bring the signal up to the shot noise limit of the detector. A survey of results from the literature showed that very few of the fast response materials measured offered real heterodyne

gain, and ones that did had inadequate measured, or estimated time response for a separate transmitter-receiver heterodyne system.

Future hope for this application of photorefractive materials lies in the development of new materials. One of the most exciting of new materials is the Multiple Quantum Well (MQW) device. These devices are essentially "designed" materials. By alternating very thin layers of semiconductor materials with specific trap states and carrier lifetimes can be designed. This allows the development of very sensitive photorefractive materials at very useful wavelengths such as 800 nm.

The MQW materials have significantly greater (orders of magnitude) sensitivity (gain-bandwidth potential) than traditional bulk semiconductors. They offer a great new potential for the field of photorefractives in general. Their primary shortcoming at this point is with regard to applications that require photorefractive gain. The device interaction length is currently limited to tens of microns. Thus, the gain length product is very limited, even if very large gain coefficients are obtained. This is not purely a fabrication limitation. Since the electric field is applied parallel to the light interaction, a long interaction would short out the spatially modulated electric fields. Multiple devices stacked serially in the light interaction direction might be an approach to provide gain length. Another potential shortcoming is the high attenuation required to achieve gain.

MQW devices generally utilize an absorption process to generate the index variation (electro-absorption) in a Kramers-Kronig type relationship. They are, thus, more complicated than the traditional photorefractive effect. They exhibit very sharp exciton absorption lines and as such are very sensitive to wavelength. This additional complexity has significant implications on system applications.

Preliminary performance of these devices has been quite impressive. Partovi et. al. measured 3 % diffraction efficiency in a MQW device at 830 nm wavelength. Wang et. al., describe some of the recent advances in this area. They achieved nearly 1000 cm^{-1} gain coefficient in experiments. This is the highest gain ever achieved in any photorefractive device. The absorption on this measurement, however, exceeded the gain. Thus, more development is required. The key point is that no other material offers the potential of these devices, but further investigation is required to assess their viability for a given application.

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